Lifetime Income Inequality: quantile treatment effect of retirement on the distribution of lifetime income.

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## Life cycle, social security and inequality

- Human Capital Earnings Function (HCEF)
  - Fanning out of earnings profiles across education groups as the cohort ages.
- Permanent Income Hypothesis (PIH)
  - Within cohort inequality evolves over life-cycle, reaching the highest levels in the old age.
  - Disparities in earnings between groups with different schooling levels grow in retirement age.
  - Reducing the share of income that is transferred through Social Security Systems increases life cycle inequality.
- Social Welfare Theory (SW)
  - By Pigou-Dalton Principal of Transfers any (mean-preserving) progressive transfer decreases inequality.



### Research questions

- What is the impact of staying longer in labor force on distribution of lifetime income?
- What is the impact of postponing retirement age on lifetime income inequality?

# Survey of Health Aging and Retirement

- Multidisciplinary cross-country longitudinal survey that collects micro data on individuals aged 50+.
- The data used in this study consists of five regular panel waves followed by two life history questionnaires of which the data were collected accordingly in 2004-2005, 2006-2007, 2010, 2013, 2015, and 2008-2009 and 2017.
- This study covers 16 European countries: Austria, Germany, Sweden, The Netherlands, Spain, Italy, France, Denmark, Greece, Switzerland, Belgium, Finland, Luxembourg, Portugal, Malta and Cyprus.
- The sample is constrained to males who at the moment of the interview are retired.

#### Lifetime income

#### Measure of lifetime income

$$Y_i = \sum_{j=1}^{R_i} \omega_j W_{ij} + \sum_{R_i+1}^{110} s_{j+1} \omega_j P_{ij}$$

#### where:

Y<sub>i</sub> - total lifetime income

 $W_{ij}$  - lifetime earnings from work at age j

 $P_{ij}$  - lifetime retirement pension at age j

R<sub>i</sub> - retirement age

 $s_{i+1}$  - probability of surviving to age j+1, predicted based on Lee-Carter model

 $\omega_i$  - discount rate ( 2% to age 50)



# Deriving lifetime earnings from SHARE

Earnings model:

In 
$$w_{it} = \alpha_0 + \rho S_i + \beta_1 E_{it} + \beta_2 E_{it}^2 + \beta_3 E_{it}^3 + \beta_4 E_{it}^4 + \varepsilon_{it}$$

where:

In wit - log of earnings

 $S_i$  - years of schooling

 $E_{it}$  - number of years of experience

Prediction equation:

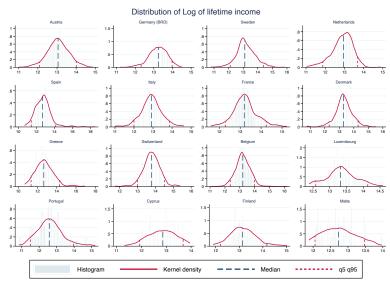
$$\widehat{\ln w}_{it+1} = \ln w_{it} + b_1(E_{it+1} - E_{it}) + b_2(E_{it+1}^2 - E_{it}^2) + b_3(E_{it+1}^3 - E_{it}^3) + b_4(E_{it+1}^4 - E_{it}^4)$$

Retransformation of predictions of earnings in logarithm to predictions in levels:

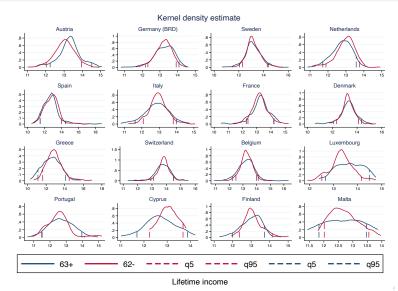
$$Q^{(p)}(y|x) = exp\{Q^{(p)}[log(y)|x]\}$$



### Kernel density estimates



## Kernel density estimates by retirement age





# Model specification

Specification of the model in a cross-country setting:

$$Y_i = \alpha_0 + \alpha_1 R_i + \beta^\top X + \varepsilon_i$$
$$Q_\tau(Y_i) = \alpha_{0\tau} + \alpha_{1\tau} R_i + \beta_\tau^\top X$$

#### where:

 $Y_i$  - personal lifetime income

 $R_i$  - binary indicator taking value 1 if an individual retired exactly at age 63 or later, and 0 if an individual retired by age 62

X - set of country and cohort dummies and education.



#### Estimation and identification

- Issues : Endogenity
- Identification: Quantile Instrumental Variables techniques
  - Abadie, Angrist & Imbens (2002)
  - Chernozukov & Hansen (2005)
- Instruments: legislated early and normal retirement ages differenced with age:

$$\begin{cases} \mathsf{Z=1}, & \text{if } \mathsf{A}_i - \textit{leg}_{\textit{ER}} \geq 3 \\ \mathsf{Z=0}, & \text{if } \mathsf{A}_i - \textit{leg}_{\textit{ER}} < 3 \end{cases}$$

where:

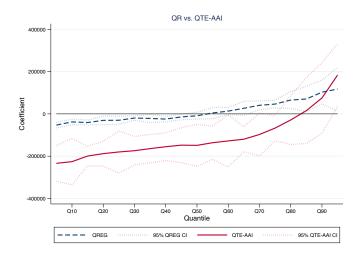
 $A_i$  is the actual age of an individual in the year of the interview,  $leg_{ER}$  is the earliest legal retirement age that an individual is eligible for.



# Ordinary Least Squares Estimates vs. Ordinary Quantile Regression

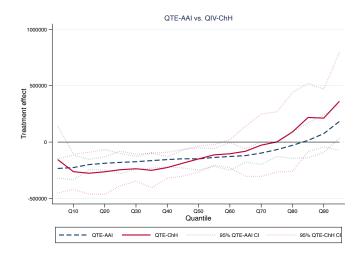


## Quantile Regression vs. Quantile Treatment Effect (AAI)





## Quantile Treatment Effect by the two estimators QTE-AAI and QIV-ChH





#### Conclusions

- Clearly heterogenous, redistributive effect of postponing retirement to later ages across the quantiles of lifetime income in the overall sample.
- Extending working lives spreads out inequality in lifetime resources.