

Rising longevity and US wealth inequality

some empirical evidence

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Income and Wealth inequality: Drivers and consequences

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Motivation

Rising longevity and wealth inequality in the US

Life expectancy at retirement \uparrow substantially

Rising longevity and wealth inequality in the US

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Up 5+ years: 14.1 years (1950) → 19.5 years (2015)

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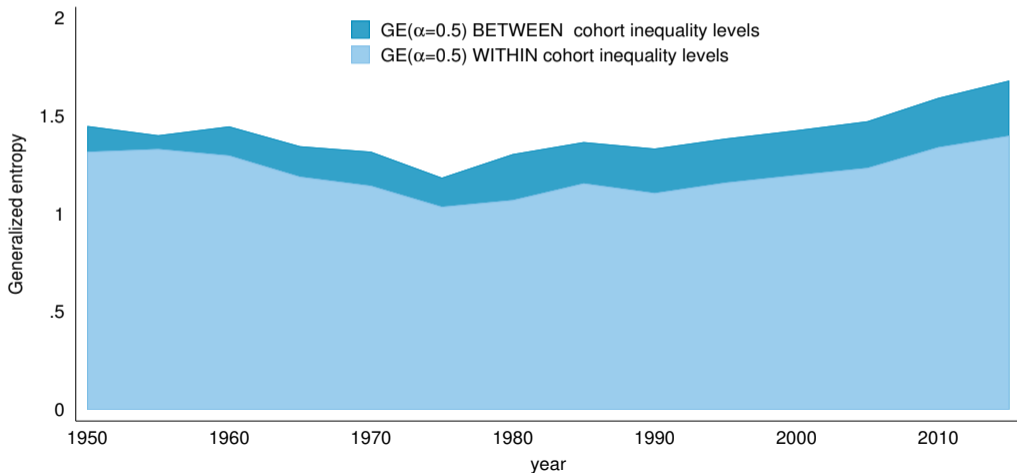
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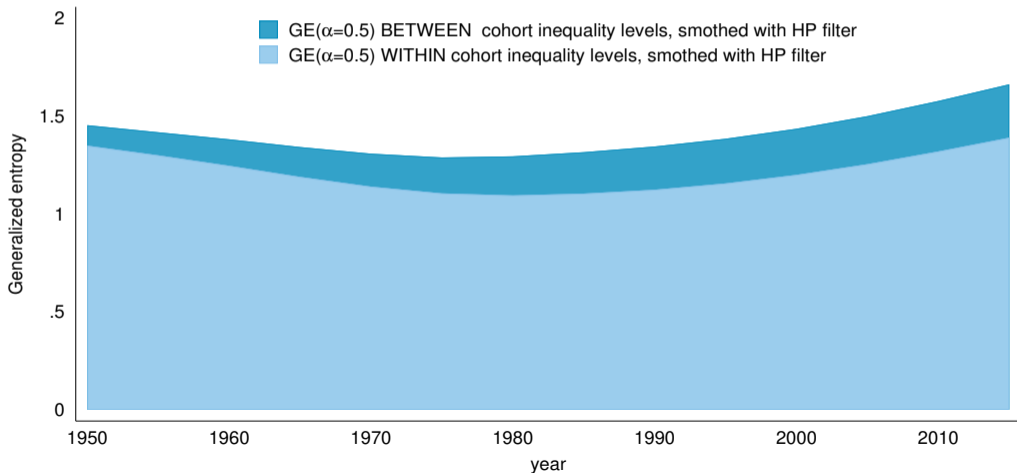
Question: does longevity matter quantitatively for wealth inequality?

→ We study wealth inequality patterns across birth cohorts (SCF data)

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 - Longer-lived birth cohorts contribute the most to inequality

Data & methods

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Demographic characteristics match Current Population Survey and U.S. Census data

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- 2 **LE65 vs $GE_{between}$** – Connect changes in between cohort inequality to changes in longevity
- 3 **RIF Regression** – We identify which cohorts contribute the most to wealth inequality

Methods – Generalized entropy:

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Methods – Generalized entropy

$$GE(\alpha) = \frac{1}{N\alpha(\alpha - 1)} \sum_{i=1}^N \left[\left(\frac{a_i}{\bar{y}} \right)^\alpha - 1 \right], \quad (4)$$

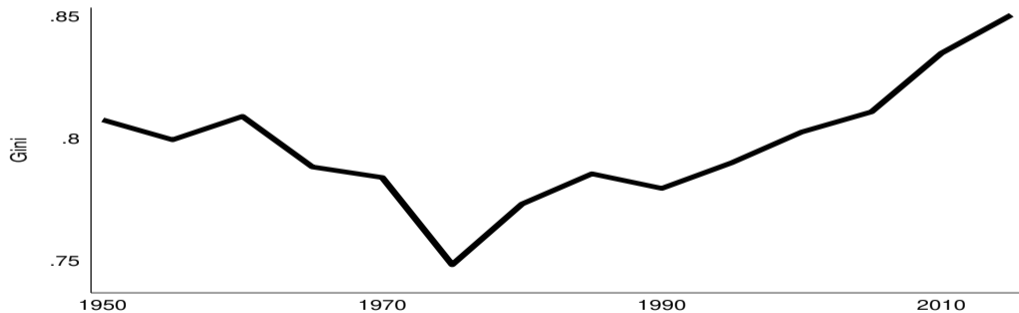
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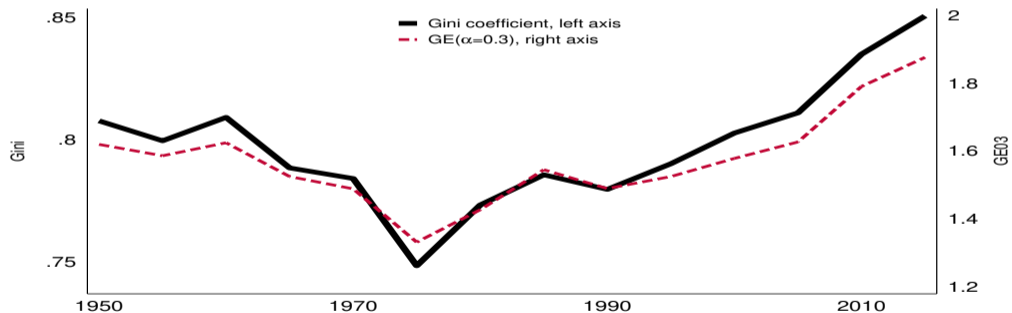
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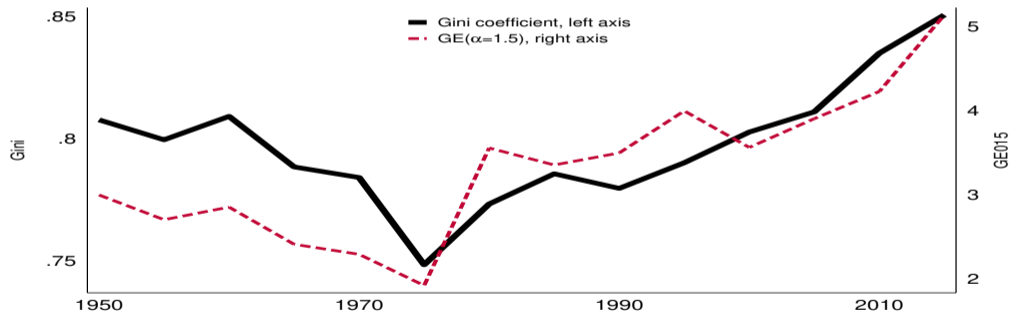
Alpha comparison



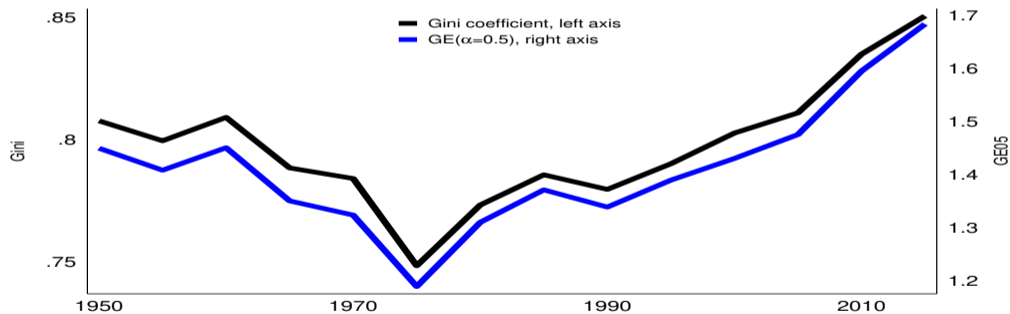
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- \bar{y}_c - arithmetic mean of assets of cohort c
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- n_c - population share of cohort c

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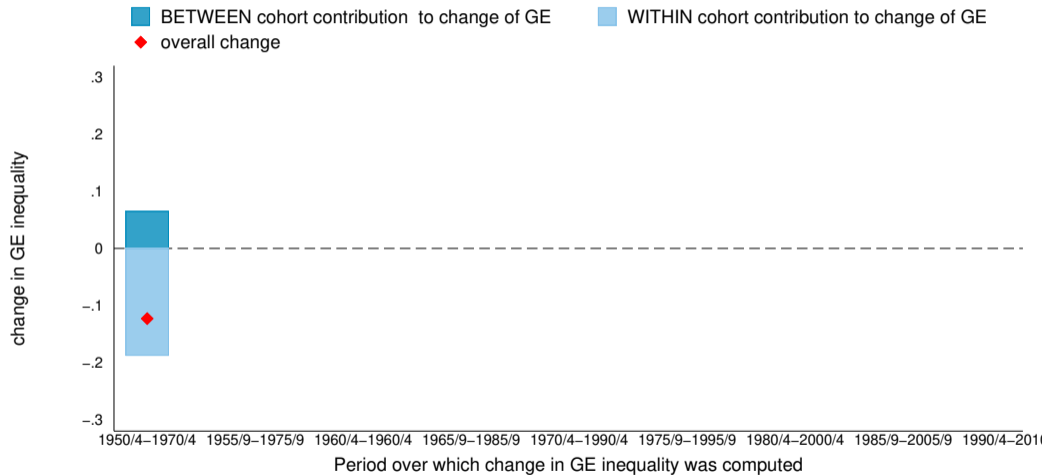
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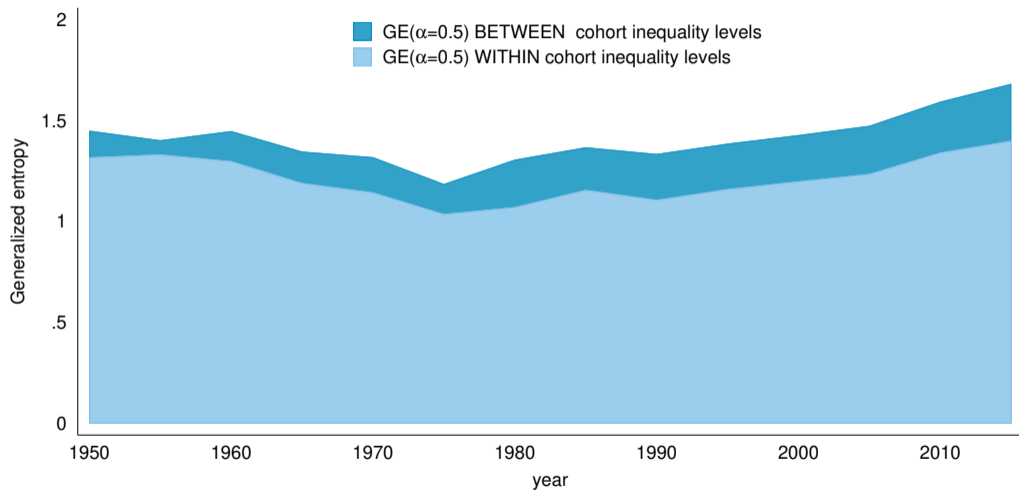
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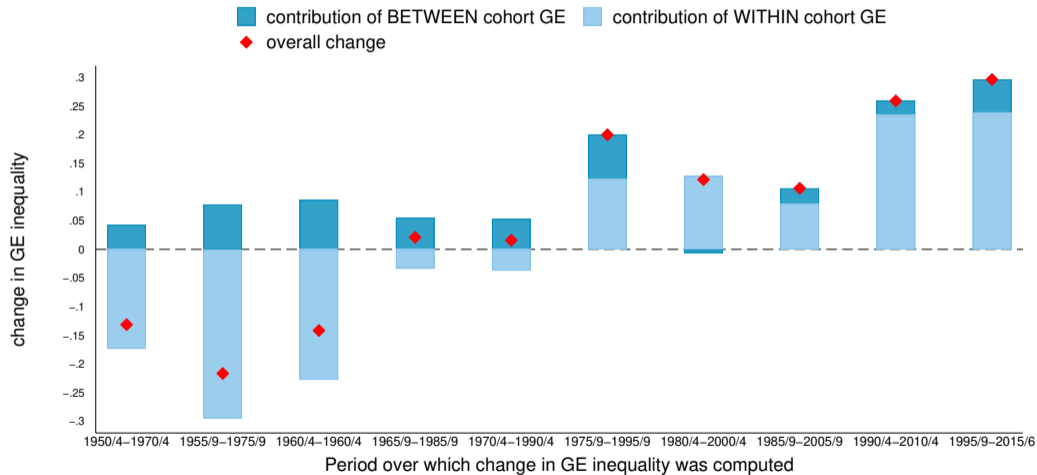
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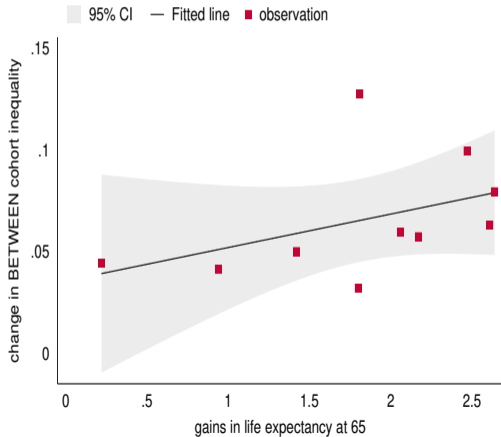
Results





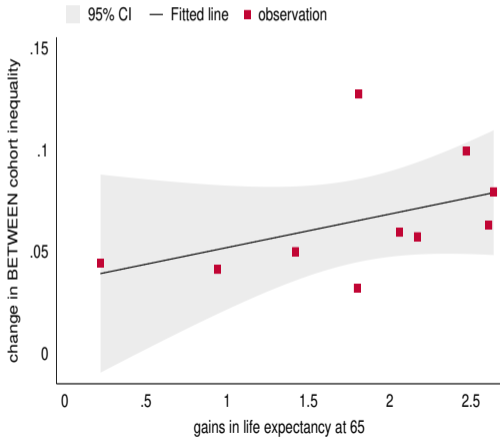


Between cohorts inequality vs LE65 changes

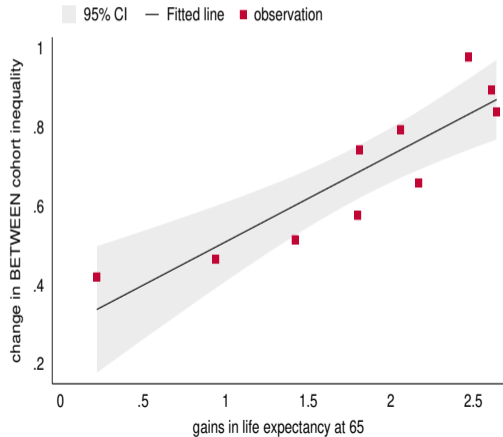


Note: Population structure fixed at 1950 level

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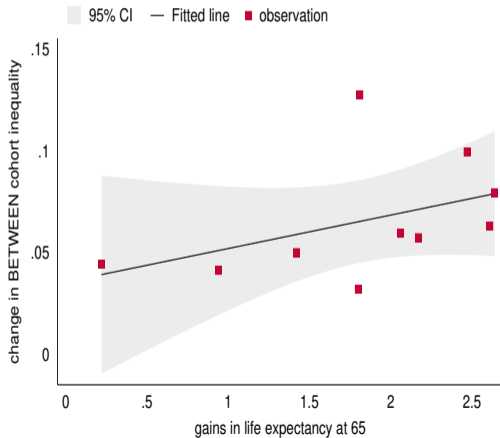


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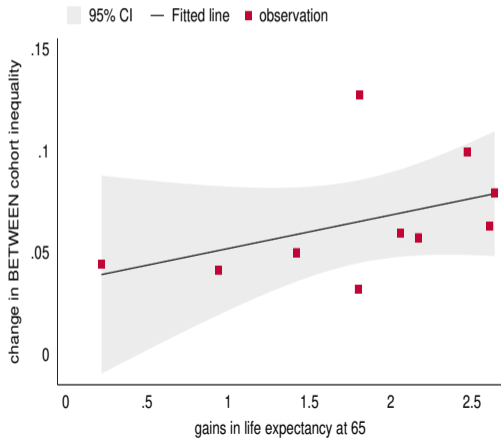
Note: Population structure fixed at 1950 level; between cohort inequality smoothed

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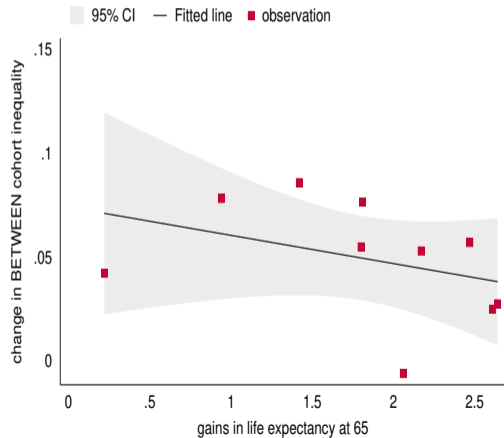


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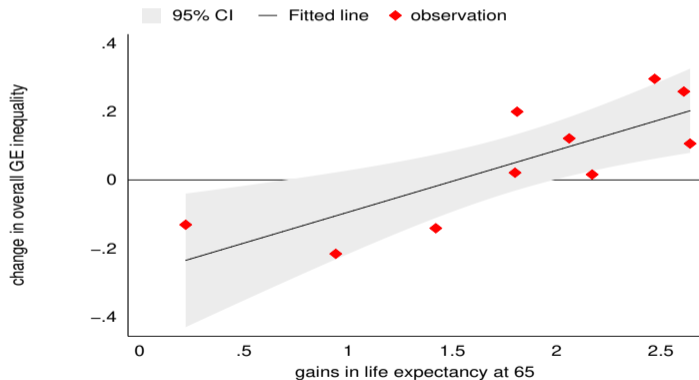


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Note: Population structure as in the data

Total inequality vs LE65 changes



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- Deaton and Paxson (1994) decomposition
- Recentered Influence Functions (Firpo et al. (2009) & Rios-Avila (2020))

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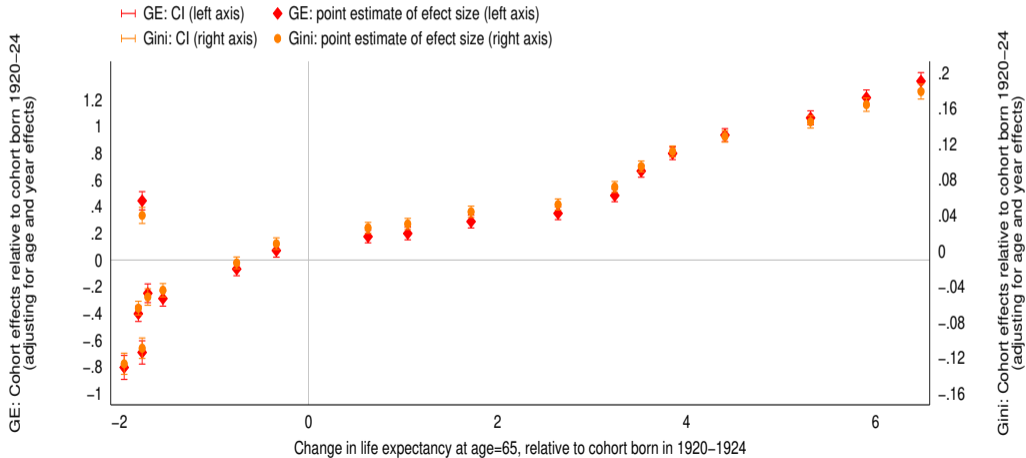
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β_c – unconditional partial effect of cohort on distributional statistics (GE/GINI)

Evolution of β_c across cohorts



Relevance

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- Structural models misspecification – **infinitely lived agents**
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- Possible policy misspecification

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Questions or suggestions?
Thank you!

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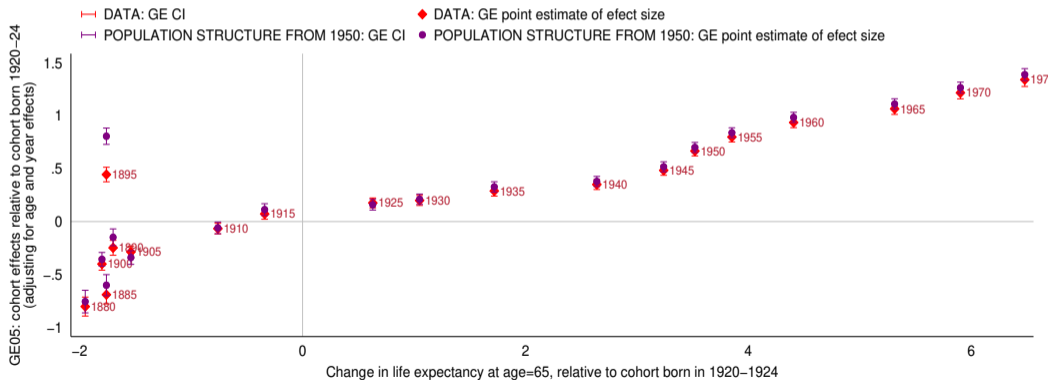
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f: [grape.org](https://www.facebook.com/grape.org)

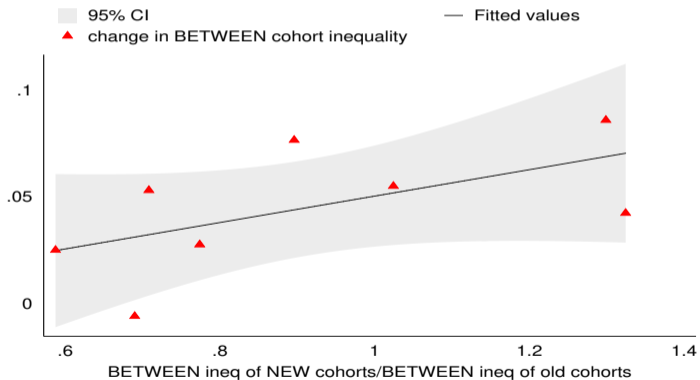
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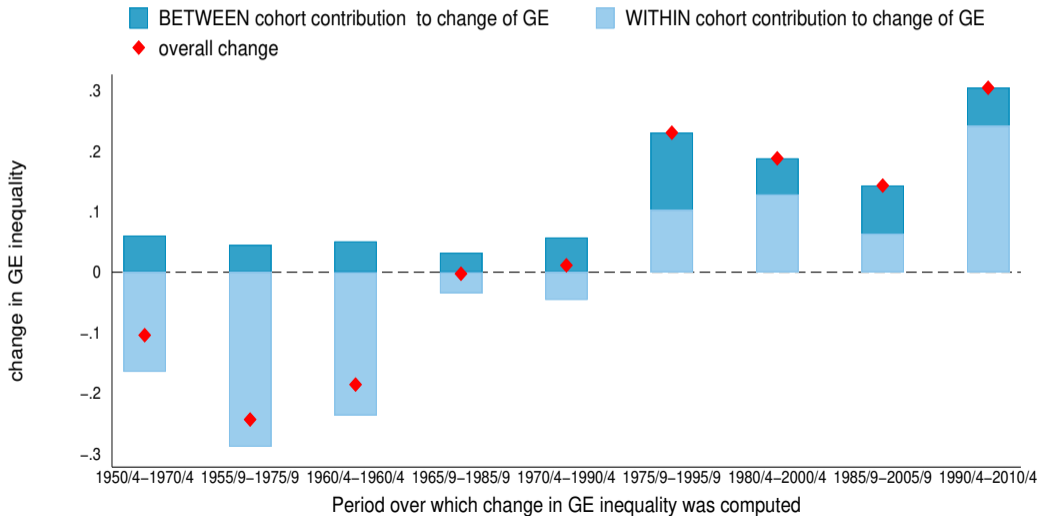
Appendix

Ratio comparison



Ratio comparison





Note: Population structure frozen at 1950

GE within

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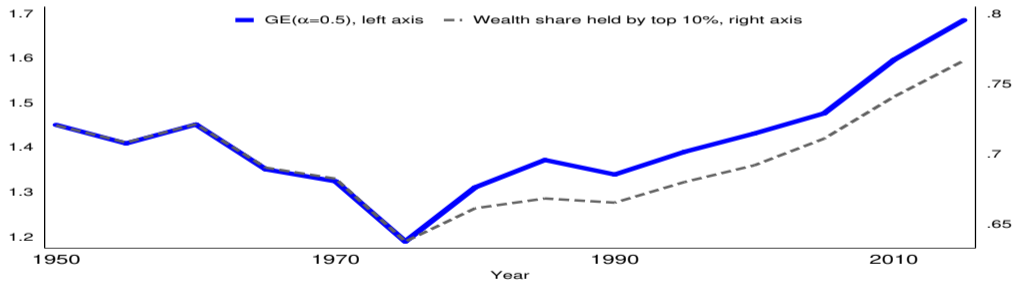
Intuition

age/year	y_1950	y_1955	y_1960	y_1965	y_1970	y_1975	y_1980	y_1985	y_1990	y_1995	y_2000	y_2005	y_2010
20	1930	1935	1940	1945	1950	1955	1960	1965	1970	1975	1980	1985	1990
25	1925	1930	1935	1940	1945	1950	1955	1960	1965	1970	1975	1980	1985
30	1920	1925	1930	1935	1940	1945	1950	1955	1960	1965	1970	1975	1980
35	1915	1920	1925	1930	1935	1940	1945	1950	1955	1960	1965	1970	1975
40	1910	1915	1920	1925	1930	1935	1940	1945	1950	1955	1960	1965	1970
45	1905	1910	1915	1920	1925	1930	1935	1940	1945	1950	1955	1960	1965
50	1900	1905	1910	1915	1920	1925	1930	1935	1940	1945	1950	1955	1960
55	1895	1900	1905	1910	1915	1920	1925	1930	1935	1940	1945	1950	1955
60	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935	1940	1945	1950
65	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935	1940	1945
70	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935	1940
75	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935
80	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930
85	1865	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925
90	1860	1865	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920

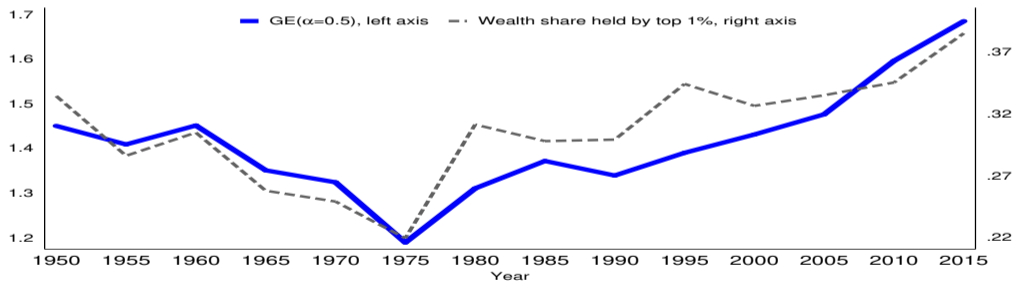
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70	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935	1940
75	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930	1935
80	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925	1930
85	1865	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920	1925
90	1860	1865	1870	1875	1880	1885	1890	1895	1900	1905	1910	1915	1920

Intuition



Intuition



Intuition

Age:	Period 1	Period 2	Period 3	Period 4	Period 5	Period 6	Period 7	Period 8
20	Cohort 7	Cohort 8	Cohort 9	Cohort 10	Cohort 11	Cohort 12	Cohort 13	Cohort 14
30	Cohort 6	Cohort 7	Cohort 8	Cohort 9	Cohort 10	Cohort 11	Cohort 12	Cohort 13
40	Cohort 5	Cohort 6	Cohort 7	Cohort 8	Cohort 9	Cohort 10	Cohort 11	Cohort 12
50	Cohort 4	Cohort 5	Cohort 6	Cohort 7	Cohort 8	Cohort 9	Cohort 10	Cohort 11
60	Cohort 3	Cohort 4	Cohort 5	Cohort 6	Cohort 7	Cohort 8	Cohort 9	Cohort 10
70	Cohort 2	Cohort 3	Cohort 4	Cohort 5	Cohort 6	Cohort 7	Cohort 8	Cohort 9
80	Cohort 1	Cohort 2	Cohort 3	Cohort 4	Cohort 5	Cohort 6	Cohort 7	Cohort 8

Bibliography

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