LIS Working Paper Series

No. 706

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July 2017



CROSS-NATIONAL DATA CENTER in Luxembourg

Luxembourg Income Study (LIS), asbl

Absolute Poverty: When Necessity Displaces Desire¹

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June, 2017

¹The main data sources for this article are the core price list for the International Comparisons Project 2011 and the regional price lists for Africa and Asia. I am grateful to the World Bank and Dr. Nada Hamadeh for access and support. These data are available to researchers upon application to the Director of the Data Development Group at the World Bank. See ICP Global Office, 2011 ICP Data Access and Archiving Policy: Guiding Principles and Procedures for Data Access, 2012,

http://pubdocs.worldbank.org/en/790491487172245068/121120-ICPDataAccessPrinciples-Pr ocedures.pdf, pp. 6-7, for details on the application procedure. I am grateful to Ligita Visockyte for exceptional research assistance and to Mattia Fochesato for programming assistance. I thank Anthony Atkinson, François Bourguignon, Shaohua Chen, Angus Deaton, Erwin Diewert, Stefan Durcan, Ian Gazeley, Rob Feenstra, Francisco Ferreira, Pablo Hernandez, Alan Heston, Sara Horrell, Dean Jolliffe, Branko Milanovich. Michail Moatsos as well as three referees and participants in several seminars for questions, comments, suggestions, and discussion.

Abstract

Robert C. Allen 'Absolute Poverty: When Necessity Displaces Desire'

A new basis for an international poverty measurement is proposed based on linear programming for specifying the least cost diet and explicit budgeting for non-food spending. This approach is superior to the World Bank's '\$-a-day' line because it is (1) clearly related to survival and well being, (2) comparable across time and space since the same nutritional requirements are used everywhere while non-food spending is tailored to climate, (3) adjusts consumption patterns to local prices, (4) presents no index number problems since solutions are always in local prices, and (5) requires only readily available information. The new approach implies much more poverty than the World Bank's, especially in Asia.

JEL codes: I12, I32, O61, O63

keywords: absolute poverty, diet problem, linear programming, World Bank poverty line

Funding: This research was supported through a research allowance provided by New York University Abu Dhabi.

The World Bank's famous \$-a-day poverty line began life as the finding of a scientific inquiry in the 1980s, became the Bank's metric for measuring poverty in 1990, and reached full maturity when it was enshrined in the Millenium Development Goals as the standard for tracking poverty around the world. However, the line rests on contestable foundations that give rise to a host of theoretical and practical problems as well as leading, we argue, to underestimates of poverty in much of the developing world.² While the World Bank poverty line (WBPL) was originally conceived for developing economies, it must now be applied to all countries in view of the United Nation's new Sustainable Development Goals, which came into effect on 1 January 2016. "Goal 1.1: By 2030, eradicate extreme poverty for all people everywhere, currently measured as people living on less than \$1.25 a day." (Atkinson 2017, p. 13). If extreme poverty is to be measured *everywhere*, then the WBPL must be revised since it is not valid outside of the tropics. This paper proposes a new method for defining absolute poverty that avoids the many problems of the World Bank's line and which makes a more robust tool for measuring extreme poverty on a global basis.

The statistical origins of the World Bank Poverty Line (WBPL) give rise to many of its difficulties. Ravallion, Datt, van de Walle (1991) were looking for a measure of absolute poverty. They collected poverty lines for 33 countries ranging from the very poor to the rich, converted the lines to US dollars with a PPP exchange rate and plotted the lines against per capita consumption. They noticed that the lines of the six poorest countries were clustered around \$1 per day in 1985 dollars, and that became their measure of absolute poverty. The dollar value was raised to \$1.08 in 1993 dollars when Chen and Ravallion (2001) updated the same data with national price indices.

The empirical base of the WBPL was greatly strengthened in the new millenium when Ravallion, Chen, and Sangraulla (2009) put together a new data set of 74 national poverty lines. Once again, poverty lines increased with income, but, in this case, no such trend was apparent in the fifteen poorest countries.³ Ravallion, Chen, and Sangraulla concluded that these lines represented 'absolute poverty'. Converting them to US dollars with PPP exchange rates produced the \$1.25 poverty line in 2005 dollars. Most recently, the poverty lines of these 15 countries in the own currencies were raised with national price indices to 2011 values and then converted to US dollars with PPP exchange rates computed from the 2011 round of the International Comparison Program (ICP 2011) price data. The average came to US\$1.88, which was rounded up to \$1.90, to give the current World Bank poverty line (Ferreira et al. 2016). Similar values have been reached by other methods (Kakwani and Son 2016, Sillers 2015, Joliffe and Prydz 2016). This 'strange alignment of the stars' has increased the line's credibility (Atkinson 2017, pp. 19-20).

The line is only as good as these procedures, and they raise many troubling issues. First, which countries should be used to define 'absolute poverty'? Should the reference group be updated? Deaton (2010, pp. 15-6) pointed out that India was in the original 1991 sample of poor countries but grew so much in the next fifteen years that it was not in the 2005 group of 15 poor countries. However, the Indian poverty line was very low, so excluding it in 2005 raised the average and the WBPL with it. This meant that the number of poor in India and elsewhere increased markedly despite India's economic growth–a perverse

²The line as been much debated. Recent contributions include Ferreira et al. (2016), Deaton (2010), Reddy and Pogge (2010), and Ravallion (2010). Related research investigates subsistence lines (Lindgren 2015) and consumption floors (Ravallion 2016).

³The countries are: Malawi, Mali, Ethiopia, Sierra Leone, Niger, Uganda, Gambia, Rwanda, Guinea-Bassau, Tanzania, Tajikistan, Mozambique, Chad, Nepal, Ghana.

result, indeed!

Second, measuring the prices is tricky. In some countries the data are nationally representative; in others, they describe major cities only. In big countries like India and China where regions are not well integrated, the relative prices for the whole country in the ICP may not represent the price structure of any of its regions. The prices come from surveying shops, but in the case of small farmers, who eat some of their crop and sell the rest, the price of their food is the price they could have sold it for–not a price in a shop. And how should we define the commodity? The ICP takes a very fine grained approach and tries to compare rice to rice (indeed, the same grade of rice) and wheat to wheat. But if the poor eat only wheat in a wheat growing country and rice in a rice growing country, might it not be better to compare the price of 'grain' and measure that as the price of wheat in the first instance and rice in the second? (Deaton 2010, p. 24) As it is, the ICP contains the prices of many commodities that have virtually no sales. The ICP 2011, for instance, reports the price of mackerel in Zimbabwe, and that is an input into the food component of Zimbabwe's PPP exchange rate, but mackerel is not eaten by the poor in this landlocked country and is probably only available in a specialized shop in Harare.

Housing presents special problems. ICP 2011 contains rental (and purchase) values for housing in some developing countries, and these are usually broken down along traditional/modern lines and whether or not they possess running water, electricity, indoor kitchens, and so forth. Location, which is of cardinal importance, is not explicitly dealt with, but presumably the rents are nationally representative. The problems in measuring the volume and price of housing services across countries are so difficult that in 2005 the volume of housing services in Africa and Asia was estimated as a constant percentage mark-up on the rest of consumer expenditures. The implied prices of housing services were highly erratic (Deaton and Heston 2010, pp. 25-6). This approach is not systematic enough for poverty measurement–especially when applied to rich countries.

Third, the usual index number issues surrounding formulas and weights bedevil both the PPP exchange rates and measurement of inflation in national statistics. Conversions from local currencies to US dollars are typically done with the PPP exchange rate for household consumption. The spending pattern of the poor differs from that of the average household: does that distort the result? Not as much as one would think (Deaton and Dupriez 2009). However, the spending pattern of the average household in Niger, for example, does differ dramatically from that of the average household in the USA. If Törnqvist-Divisia indices are used, then the US shares are averaged with Niger's to form the weights. These weights will bring into the calculation many goods and services that are never consumed by Niger's poor (Deaton 2010, pp. 22-4).

Fourth, the existential meaning of poverty depends on the national poverty lines in the group defined as poor. What is their content? The poverty lines in the original Ravallion Ravallion, Datt, van de Walle (1991) study did not exhibit a common standard (Allen 2013). The sample of poverty lines for the 74 countries underlying the 2005 poverty line is put together more systematically. The usual procedure involves four steps. First, a calorie requirement is set. 2100 calories per person is often used, but, in fact, there is considerable variation. Second, using data from a household expenditure survey for the country, find a band of the income or consumption distribution where average calorie consumption equals the chosen standard. Third, set the poverty line equal to the income or consumption per head for the band choosing the calorie standard. The 'food' budget is what is spent on food and the rest of spending is 'nonfood'. No effort is made to investigate these aggregates further. Fourth, convert this national poverty line, which is in local currency, into US dollars with a

PPP exchange rate.

Many features of this procedure are problematic. First, should a uniform calorie standard be set or should it vary over time and across space (reflecting differences in work intensity) or demographic structure? In the event, a uniform calorie standard is not maintained. Atkinson (2017, p. 128) found that it varied between 2030 and 3000 calories per adult in 10 poor countries, raising obvious questions of comparability. Second, how adequate is the rest of the food budget in terms of protein, fat, vitamins and minerals? Is it austere or luxurious? Third, how Spartan should the non-food budget be? How should it vary with climate? Since most of the fifteen poor countries are in the tropics, it is unlikely that the average non-food budget includes enough fuel and clothing to survive a Russian winter, for instance. Finally, even though the procedure is clear, it suffers greatly from a lack of transparency. Since the Bank does not explore and assess what makes up 'food' and 'non-food' spending, there is no persuasive answer to the question 'how can you live on \$1 a day?' Indeed, we show that people in the USA, the UK, and France could not live on the 2011 version of that line.

The World Bank is committed to ending "chronic extreme poverty by 2030." To know if it is succeeding, the Bank must measure poverty, and, in view of the many difficulties in so doing, it "convened a high-level Commission led by Sir Anthony Atkinson...to advise the World Bank on the methodology currently used for tracking poverty in terms of people's consumption, given that prices change over time and purchasing power parities across nations shift."⁴ While Atkinson was aware of the many difficulties with of the current poverty line and favoured further research to improve it (including the approach of this paper), he never-the-less endorsed the continued use of the local currency equivalents of the \$1.90 line with the only adjustment being to raise them over time in line with inflation in local prices. There are two reasons for this approach. First, Atkinson's terms of reference were narrow. "The Commission was asked to take the 2015 estimates as its point of departure and to assess how the process may be carried forward to monitor progress up to 2030 in achieving SDG goal 1.1." Second, "the \$1.90 [line] has acquired an independent political status." Better to stick with imperfect goal posts rather than muddle the scoring by shifting the goal posts in the middle of the match. (Atkinson 2017, pp. 22, 30, Ferreira et al. 2016.)

While Atkinson's recommendation makes administrative sense, it does not resolve the underlying scientific and philosophical difficulties. Ideally, the international poverty line should satisfy five criteria: (1) It should have a clear meaning related to survival, health, and well being. In terms of Sen's (1987, 1992) theory of capabilities, the poverty line should sustain basic functionings like being active, growing, and healthy. The line should also (2) represent a constant standard across time and space, (3) respond to local prices and other pertinent local factors like climate, (4) avoid intractable index number problems, and (5) require only readily available information.

This paper develops an approach that satisfies these requirements. The paper operates on both the normative and the positive plane. On the normative plane, I propose that the poverty line be set by explicitly budgeting for basic needs. This is a long standing tradition that is still widely used in Europe and the USA when 'reference budgets' are drawn up to specify poverty lines (Rowntree 1901, Goedemé et al. 2015, Carlson et al 2007.) The Basic

⁴These quotations are from the Forward to the report by Kaushik Basu, Chief Economist and Senior Vice President of the World Bank Group (Atkinson 2017, p. vii).

Needs Poverty Line (BNPL) developed here has three categories of spending-food, non-food goods, and rented housing. My approach uses linear programming to set the diet portion of the poverty budget and early twentieth budget studies for industrial workers in St. Petersburg and Bombay to make non-food spending climate dependent. Housing is also explicitly budgeted. This approach avoids all of the problems of the World Bank's methodology. I illustrate the method here using a sample of twenty countries ranging from Niger and Zimbabwe to France, the UK, and the USA.

An objection to linear programming diets is that they are unrepresentative of actual behaviour and so of no use in setting a poverty line or for any other practical purpose. The second plane on which the paper operates is positive and aims to assess the predictive power of linear programming diets. I agree with the conventional view (Stigler 1945) that linear programming utterly fails to explain the diets in rich countries. It is a different story in developing countries, however. Linear programming does a reasonable job in explaining the total quantity of food and its distribution among broad categories. The linear programming diets are predominantly vegetarian. Grain bulks very large. Small quantities of animal proteins and oil are also consumed. Linear programming usually predicts the predominant grain consumed in a country. It cannot predict the variety of fruits and vegetables that the poor eat, nor can it explain the universal consumption of small quantities of sugar nor eating associated with festivals. There is a small amount of 'wiggle room' in which people have some space to consume a little sugar, favourite spices, or traditional foods at the expense of a healthy diet. But it is the nature of poverty that the latitude for these substitutions is limited–certainly in comparison to rich countries.⁵

Specifying the poverty line diet with linear programming

The diet problem was the first linear programming problem ever formulated in a famous paper by Stigler (1945). The problem is to choose a diet from a list of foods that minimizes the cost of meeting a set of nutritional requirements. The objective function to be minimized is the cost of the diet:

$$Cost = \sum p_i F_i \tag{1}$$

where p_i is the price of a food and F_i is the quantity of the food consumed. The summation can extended over a list of t foods $F_1...F_i$, many of which will not selected in the solution.

The nutritional requirements are specified with a set of inequalities, each of which sets the requirement for one nutrient.

$$\sum n_{ji} F_i \ge R_j \tag{2}$$

Here the summation also runs over all of the foods indexed with i. R_j is the required amount of nutrient j-the minimum calorie requirement, for instance. n_{ji} is the quantity of nutrient j per unit of food F_i , for instance, n_{ji} might be the number of calories per kilogram of wheat flour and F_i , the kilograms of wheat flour in the diet. Each nutrient required in the diet has an inequality describing that requirement.

Finally, the consumption of each food has to be at least zero:

⁵This is a specific sense in which economic development creates freedom (Sen (1999).

$$F_i \ge 0$$
 for all i (3)

The linear program model presents a neat contrast to the standard model of consumer choice in its dual form. In that form, consumer goods are chosen to minimize the cost of meeting a specified utility level U*. The difference with the linear programming model is that the inequalities (2) are replaced by the utility constraint, equation (4) :

$$U(F_1...F_t) \ge U^* \tag{4}$$

This is the formal sense in which necessity displaces desire in the definition of absolute poverty.

These days, linear programs can be easily solved with the simplex algorithm in Excel. The solutions have two properties that are important for defining the poverty line. First, increasing the number of requirements or increasing the magnitude of a requirement either leaves the cost of the diet unchanged or increases it. A more nutritious diet is never cheaper than a less nutritious diet and may well cost more. Second, the maximum number of foods that solves the problem is equal to or less than the number of requirements. The number of requirements, therefore, limits the variety of the diet.

In his original investigation of the diet problem, Stigler (1945) used US prices from 1939 and 1945 to compute the cost of the least cost diet meeting a set of requirements including calories, protein, iron, niacin, calcium, vitamin C, vitamin A, thiamine, and riboflavin with values appropriate to a 'moderately active' man weighing 154 lbs. Stigler did not have Excel at his command but nevertheless reasoned his way to almost the correct answer. The solution for 1939 was 168 kg of wheat flour, 129 kg of dried navy beans, 23 kg of evaporated milk, 50 kg of cabbage and 10 kg of spinach. The values warrant comparison with ones we compute for developing countries in 2011.

Stigler's reaction to the solution has also been important: he thought the diet was impractical. "No one recommends these diets for anyone, let alone everyone; it would be the height of absurdity to practice extreme economy at the dinner table in order to have an excess of housing or recreation or leisure." (Stigler 1945, pp. 312-3) This theme has been taken up by subsequent economists, who have tried to incorporate 'palatability' into the program. Smith (1959, p. 272) remarked that Stigler's diet was "a dramatic illustration of how little purely nutritional needs have to do with the level of actual food expenditures...If we want diets that someone might be willing to eat, we need models that take account of tastes and habits." This is surely true of people in rich countries whose behaviour is determined by preferences, income, and prices. Linear programming is much more germane to poor people, however. For them, survival is the issue, and the needs for survival take precedence. Preferences and income give way to nutritional requirements in determining consumption with prices still playing a role. Indeed, from the linear programming, rather than standard consumer theory.

'Nutritional requirements' has an aura of scientific objectivity, and Stigler (1945) and Smith (1959) adopted lists of requirements issued by nutritional boards without criticism or examination. Indeed, it was the desire for an objective standard for poverty that motivated the research described here. However, it is clear on examination that the nutritional requirements set by bodies like the World Health Organization are in important respects subjective.⁶ First, precise values for some nutrients such as calories and protein can be specified with reasonable accuracy, but for others that is not possible. Niacin, for instance, is necessary to prevent pellagra, and field observations suggest widespread appearance of pellagra in populations where adult men receive less than 7 mg of niacin per day. However, the current WHO requirement for adult men is set at 21 mg on the grounds that the higher value contributes to better health (Prinzo 2000, p. 11, Rao 2009, pp. 256, 260). The poverty line distinguishes the 'poor' from the 'non-poor'. Should the line be set at 7 mg or 21 mg or somewhere else? I have adopted the recommendations of the medical authorities, but the uncertainties should be recognized. Second, for this reason, most of the world's population is deficient in some nutrients. 90% of the Indian population, for instance, is anaemic by current standards, which means they are deficient in iron, thiamine, or folic acid. Evidently, many 'non-poor' are deficient in these regards, so that full adequacy with respect to iron does not distinguish the poor from the non-poor. Perhaps 'moderate anaemia' should be the dividing line with correspondingly reduced nutritional requirements? Third, for geographical reasons, some required nutrients are not available to most of the world's population. Iodine, for instance, is naturally available only to people living near oyster beds. Unless iodized salt is available, most people in the world would be iodine deficient, so there is no point including it as a requirement in a programming model defining a poverty line. Fourth, none of these standards takes into account the seriousness of the impairment to life that results from the deficiency. It may be that most people are unconcerned about vitamin A deficiency because night blindness does not appear a costly disability-at least not sufficiently detrimental to require the expenditure necessary to eliminate it.

These uncertainties affect the linear programming approach to diet in two important ways. First, we omit from consideration nutrients whose availability are locationally specific. Iodine is an example, as is vitamin D. People are not vitamin D deficient in sunny climates, although they may be deficient in cloudy, wet places. The poverty line is meant to distinguish the poor from the better off, and the availability of iodine and vitamin D does not do that.

Second, with respect to other nutrients, the linear programming approach takes on the character of an estimation exercise rather than a purely objective determination of the optimal diet. One question we ask is whether there is a set of nutritional standards that is common across the world and that rationalizes the diets that poor people consume. We argue that the answer is (approximately) yes, and that is the standard incorporated in our measure of poverty. In this sense, the choices made by the poor imply the poverty line: The poor have a voice in defining poverty–even if they are not aware of it.

Data and empirical specification

To compare our results to the World Bank's poverty line of \$1.90 per day in 2011, we need prices from 2011. The principal data source is the ICP2011 core spreadsheet and the regional spreadsheets for Africa and Asia.⁷ The ICP is a tremendous achievement, but it was

⁶For a list of relevant WHO publications, most available online, see http://www.who.int/nutrition/publications/nutrientrequirements/en/

⁷The core prices were taken from *ICP2011: Data for Researchers*, the African prices from *ICP2011_AFR_Regional2011*, and the Asian from *ICP2011_ASI_Regional2011*. I am

necessary to fill some lacunae and add accommodation rental prices derived from other sources (See Appendix). I investigate the implications of these prices for 20 countries ranging from the poorest to the richest (Table 1 onward).

Countries are a natural unit of analysis since poverty is a national political issue and since countries share a common currency, but there are also reasons for choosing a regional approach. Prices differ across regions in large countries with poor infrastructure or other impediments to trade, and those differences imply different poverty lines. Climate also varies within countries. The World Bank has set different lines for urban and rural parts of India, China, and Indonesia. However, it is not possible to explore these issues using the ICP, which is the basis for international comparisons, since it reports only one price for each good in each country. When regional issues look likely to be important, they will be noted.

least cost diets: 1700 calorie model

We begin by examining the diets implied by various nutritional requirements.⁸ We consider them in an increasingly stringent progression. There are four models in the sequence. Each contains all of the nutrients of the previous step and increases the quantity of those nutrients or adds additional nutrients or both.⁹ The models are:

- **1700 calorie** model. The only requirement is 1700 calories per day.
- **CPF** model. Three nutrients are required: 2100 Calories per day, 50 g. of Protein, and 34 g. of Fat
- **basic** model. CPF requirements plus the Indian recommended daily allowances (RDA) of iron, folate, thiamine, niacin, and vitamins C and B12.
- **full course** model. Basic model plus RDA of six more vitamins and minerals.

We begin with the most elementary requirement–calories. What is the minimum cost of a diet that supplies just enough calories for survival? By 'survival' we do not mean the minimum for a single adult to subsist from one day to the next but rather the minimum, on average, for the species to survive. Adults must have enough energy to work and children to grow.

The minimum society-wide average can be established in two ways. One is by calculation.¹⁰ The distribution of the population by age and sex is determined, and the energy

⁹Details about the linear programs are found in the appendix 'notes on the linear programming.'

¹⁰FAO (2001) explains the methodology.

grateful to Nada Hamadeh and the World Bank for making these data available to me.

⁸Each requirement is expressed as an inequality in the form of equation (2). The quantity of each nutrient per kilogram of food (n_{ji}) must be specified. Generally the values used were those shown on the US Department of Agriculture, *National Nutrition Database* website. Some values, however, were taken from the regional nutritional databases listed in the online references. These data bases often do not agree with each other, and it might be important to investigate these discrepancies, but that has not been done here.

required for basal metabolism for each age-sex group is calculated with standard formulae. The results depend on the average height of each group and the Body Mass Index that each is expected to maintain. Additional allowances are also required for pregnant and lactating women. Basal metabolism of each group is then increased by its physical activity level (PAL). Determining the PAL requires constructing an activity schedule across the year, so that the appropriate mark-up can be applied to each hour (the physical activity ratio or PAR) depending on exertion. More strenuous activities get higher PAR's. The PAL can then be computed as the average of the PAR's over the year.

Calculations along these lines point to around 2000 calories per person per year as the average requirement. This provides enough for some people to work very hard and for children to have enough energy to grow. The requirement varies depending on the age distribution of the population: faster growing populations have more children and a lower average calorie requirement. Calculations by the Food and Agricultural Organization (2008, p. 8) indicate a requirement of 1600-2000 calories per person per day. The US Department of Agriculture (2010, p. 2) uses a standard of 2100 calorie per person per day (with an unspecified variation across regions) in assessing food security. I have computed the same figure for Britain in 1841 assuming that the average man was a carpenter and the average woman a domestic spinner (Allen 2013).

An issue that arises with respect to energy requirements is the question of whether the shift from farm work to urban work as well as the mechanization of farm tasks has led to reductions in the need for calories (Deaton and Drèze 2009, pp. 57-8). Probably not by much. The model of Britain in 1841 can be used to calculate bounds by comparing the average energy requirement (a) if all men performed strenuous work on a continuous basis with the requirement (b) if half performed moderate work and the other half light work. Energy consumption averaged over the population drops by about 250 calories per day. This drop must overstate the actual change since not all men did strenuous activity all of the time in the 'olden days,' but it is difficult to explore this further in the absence of detailed information on work intensity and how it has changed. I have made no adjustment for this effect.

The second approach to determining calorie requirements is to look at what people actually consume. Survey data for India shows that the poorest decile of the population consumes about 1450 calories per person per year (Deaton and Drèze 2009, p. 47, Suryanarayana 2009, p. 35). This is below basal metabolism, so it is either an error, or it indicates an unusual demographic structure (which means it is not relevant for society as a whole), or the population is dying out (in which case the standard is too low).

The second decile from the bottom consumes on average 1700 calories per person per day (Suryanarayana 2009, p. 35). This is just above the lowest FAO value and about the bare minimum a group requires for survival.

In view of these considerations, linear programming diets were calculated with the only constraint being 1700 calories per person per day. The implied diets are in Table 1. With only one constraint, there can be only one food in the solution to the programming problem. For 12 countries that is a cereal or flour (170-178 kg/year depending on the kind or about a pound per day). For the other eight, it is vegetable oil (70 kg/year or about one cup per day). These are small quantities, which suggests that people eating them might be hungry. The solutions of the linear programs are in kilograms of the various foods, and the total provides a rough indicator of nutritional intake that we use to gauge the effect of increasingly stringent nutritional requirements. Total weight of a diet also provides a summary statistic to compare predicted consumption with actual diets.

The appearance of oil is unexpected, and it is probably also a recent phenomenon in world history. It reflects the widespread cultivation of palm oil in south Asia, a development of the late nineteenth century. Before that, rice or some other grain was the cheapest source of calories around the Pacific Ocean.¹¹

It is a tricky question whether man can live by maize alone, but surely he cannot live solely on vegetable oil. Aside from fat, it supplies no nutrients. A population could not survive on the vegetable oil diet. Requiring only calories leads to death rather than survival.

Least cost diets: CPF model

More satisfactory diets are implied by imposing more requirements. The second class of requirements are the principal nutrients-calories, protein, and fat. In the calculations, we increase the calorie requirement to the USDA value of 2100 per day. This allows people a more ample supply of energy to do the work that sustains society as well as raising children. Protein is set at 50 grams per person per day. The ultimate basis of this value is experiments that measure the nitrogen intake required to match the body's excretion of nitrogen and thus to maintain the body's nitrogen stocks. Fat is set at 34 grams per person per day, the amount that supplies 15% of the energy intake (FAO 2008c, p. 14). These requirements depend on body mass, age, sex, pregnancy, lactation, and so forth. In these cases (as with all other nutrients to be considered), the value of the requirement used in the linear program is calculated from age and sex specific requirements as a society-wide weighted average using the age and sex distribution of the Indian population as weights.¹² Recommended values for India are used, as they are more likely to reflect conditions in developing countries today than global recommendations.¹³ The protein requirement lies at about the 30th percentile of the Indian income distribution, while the fat requirement is in the middle (Suryanarayana 2009, pp. 35-6).

Tables 2 and 3 summarize key features of the diets as functions of the nutrient requirements. Table 2 shows average annual food consumption in kilograms. With the 1700 calorie diet, the average was 131. This increased to 200 kilograms with the CPF diet. The number of foods in the diet also increased (Table 3). There was only one food chosen with

¹³The RDAs include an allowance for losses during cooking. "Considering the cooking loss of 50%, the RDA of ascorbic acid has been set at 60 mg/day." (Rao 2009, p. 287). An advantage of using Indian RDAs is that the cooking losses are assessed in terms of Indian culinary practices, which are probably more representative of developing, tropical countries than the cooking practices in the West. See Rao (2009, pp. 14, 246, 248, 251, 257, 262, 272, 274, 275, 279, 286) for more examples.

¹¹Linear programs like those reported in this paper have been run with price data collected by Lockyer (1711, pp. 148-151) in Canton in December, 1704. Rice rather than oil was the solution to the 1700 calorie model, indicating that oil was a more expensive source of calories than rice.

¹²The nutritional requirements are from Rao (2009, pp. 105-6, 124, 119-32) and the population structure from <u>http://esa.un.org/unpd/wpp/Excel-Data/population.htm</u> There is more variation in the recommendations of professional bodies regarding fat than for other nutrients, and I have opted for a low requirement.

the 1700 calorie diet. The linear programming solution allows up to three foods with the CPF diet. Three foods are chosen in eight cases and two foods in twelve for an average of 2.40 foods.

The diets that solve the linear program with the principal nutrients as constraints are shown in Table 4. Consumption of oil is cut dramatically to plausible levels, and some is used everywhere. Wheat is the staple in wheat growing areas, as is rice in southeast Asia, and millet, sorghum, or maize in sub-Saharan Africa. Legumes are consumed in six of the cases including all of the rice based diets. It is significant that the diets are purely vegetarian, and that no alcohol, sugar, or vegetables (other than the legumes) are consumed. There is no sugar, no alcohol, and very little meat in any of the diets implied by linear programming.

Least cost diets: basic model

While the CPF diets provide better nutrition than the 1700 calorie diet, they none-theless suffer many deficiencies. We begin with those that could lead to four of the most common and serious deficiency diseases. Pellagra is due to insufficient niacin, beri-beri to a lack of vitamin B1, scurvy to insufficient vitamin C, while anaemia can be due to inadequate levels of either iron, thiamine, or folate (folic acid). Table 5 reports nutritional consumption relative to recommended daily allowances for these nutrients in the CPF diet.

In most cases, the CPF least cost diets meet the requirements for calories, protein, and fat exactly, and, when the requirements are over fulfilled, the excess is minor. So far as the minerals and vitamins are concerned, the diets supply no vitamin B12–this is found only in animal products–and none or only negligible quantities of vitamin C. The absence of vitamin B12 means that anaemia would be widespread unless consumption of B12 were inadvertent. In India, "since populations subsisting essentially on foods of vegetable origin do not show evidence of widespread vitamin B12 deficiency, it is speculated that polluted environment and unhygienic practices could be providing the necessary minimal vitamin B12." (Rao 2009, p. 278) The lack of vitamin C implies widespread scurvy.

There is a likelihood of other deficiency diseases as well. Two kinds of diets are particularly deficient. The first are the rice-based diets deduced for Vietnam and Myanmar. These diets have low enough niacin levels to suggest wide-spread pellagra and low B1 levels indicating a risk of beri-beri. It is significant that the short-grain, milled rice which they consume is particularly lacking in these nutrients. In contrast, the brown rice consumed in Sri Lanka supplies more niacin and thiamine, so the deficiency problems are not so severe.

The second kind of diet that indicates a likelihood of deficiency diseases is the wheat -based diet of France, Algeria, and Lithuania. Refined wheat flour in these countries is not enriched, so it lacks niacin and thiamine. Otherwise similar diets in the USA, UK, Turkey, and Mexico do not lead to these inadequacies because the enrichment of wheat flour is mandatory. The comparison indicates the benefits of mandatory food fortification.

In terms of the linear programming, the deficiencies can be cured by imposing the requirements on the solution. As noted previously, we compute the requirements from the Indian recommended daily allowances by computing the weighted average of the RDAs for the various age and sex groups. The results are shown in Table 6.

The additional requirements have major implications for the linear programming solutions. The first is that the volume of food consumed over the year goes up from 200 kg with the CPF diet to 344 kg. More food gives more nutrients.

The second change is an increase in the number of foods from 2.40 on average in the CPF diet to 5.00. The increase is due mainly to the addition of an animal product and a

vegetable. Animal products enter the solution as a consequence of requiring vitamin B12. The linear programming solution generally implies either the cheapest available fish–usually mackerel–in coastal districts or milk in inland regions. Meat in any form rarely appears in the solution to a linear program. The appearance of vegetables–most commonly cabbage–or cassava is due to the vitamin C requirment. The B12 and C requirements are independent of the others, so adding these requirements to the program has scant impact on the rest of the diet. Qualitatively, the pattern of food consumption is similar in the CPF and reduced basic model. The same grains are generally consumed in the same regions. Total food consumption rises because of the introduction of animal protein and vegetables.

The increase in total food consumption has another implication that becomes increasingly important, namely, the overshooting of requirements. With the CFP diet, most solutions meet the calorie, protein, and fat constraints exactly. The average degree of overshooting is only a few percentage points. Overshooting is more widespread with the basic diet. Three of the solutions overshoot calories, and the average excess is 7%. Virtually all of the diets overshoot protein, and the average excess is 32%. Most solutions meet the fat requirement exactly, but the requirement is nonetheless exceeded by an average of 13%.

full course model

The vitamins and minerals considered thus far are only a subset of all of the nutrients that might be considered. Recommended daily allowances have been set for many others. To explore the implications of some of these, requirements for vitamin A, B6, riboflavin, calcium, magnesium, and zinc have been added to the linear program.

The exercise has a surreal air because of difficulties in defining and assessing deficiencies. In the case of vitamin B6, for instance, it is difficult to measure the extent of deficiency in the population (Rao 2009, pp. 260-3). Setting RDAs is difficult in some cases (vitamin B6) and fraught with conflicting considerations in others. Calcium requirements depend on vitamin D and protein intake. Low protein consumption reduces calcium requirements meaning that standards set for rich people are too high for poor people, and by some measures most Indians look like they get enough calcium. On the other hand, femur fractures occur at younger ages amongst poor women in India suggesting there might be an issue about calcium adequacy after all. (Rao 2009, pp. 158-9) At what level should the calcium RDA be set? In other cases, it is not clear how serious the deficiencies might be. A lack of vitamin A leads to night blindness, but how costly is that? (Rao 2009, p. 296) In other cases, deficiencies are so common or so rare that the intake of the nutrient provides little information about poverty or wealth. Thus, "dietary deficiency of riboflavin is rampant in India...only about 13% households meet the dietary requirement." (Rao 2009, p. 251) In contrast, "the available reports...in India...do not report any widespread zinc inadequacy." (Rao 2009, p. 225). In neither case, does the RDA provide a boundary that distinguishes poor people from better off people.

Introducing these additional vitamin and mineral requirements implies increased food intake. The number of foods in the diets rises from an average of 5.00 with the basic diet to 6.4. In addition, more nutrients are obtained by increasing the quantity of food consumed in a year from an average of 344 kg with the basic diet to 426. The increase is greatest among the developing countries where average food consumption rises to 440 kg. The Chinese diet reaches a staggering 763 kg. Increasing the volume of food to this extent leads to considerable overshooting of calorie requirements (by 10%) and especially protein requirements (by 39% on average).

Comparison of the details of the full course diet (Table 7) to the basic diet (Table 6) shows some unusual changes. The consumption of wheat flour falls, while the consumption of legumes, cassave, vegetables and potatoes reach extreme limits. These features raise questions about the empirical relevance of the diets.

The full course diets have affinities with Stigler's original linear programming diets. The same foods turn up, and the quantities are of similar magnitudes. The reason is that Stigler's nutritional requirements include calories and protein as well as most of the vitamins and minerals considered here. Stigler's specification did not include a fat requirement, and its absence explains why there is no oil or butter in his solution.

Linear programming diets and the diets of the poor

Stigler warned us that linear programming diets provided no guidance for the behaviour of Americans, and indeed, the solutions he found do not described what Americans ate in the 1930s and 1940s. Does this judgement apply to people in 'absolute poverty' in developing countries today? With some qualification, the answer is no. Linear programming explains many features of their behaviour.

We have examined a range of four linear programming solutions reflecting different levels of required nutrition. Not all of these explain behaviour. For many countries, a pure vegetable oil diet was the solution for the 1700 calorie diet. That diet cannot sustain life and no one consumes it. The CPF diet looks more promising, but it does not include any animal products or any fruits, cassava, or vegetables (with the exception of beans in the rice based diets). Most vegetarians consume dairy products or eggs, and fruit and veg are almost universally consumed, as will be shown, so the CPF diet does not describe human behaviour well. At the other extreme, the full course diet predicts too much food consumption. 440 kg per year greatly exceeds per capita consumption in much of the world in the 1960s and so does not describe what the poor were eating. We are left with the basic model as the best candidate for describing behaviour.

We can compare the predictions of the basic model with food consumption to assess its merits. Ideally, one would test the model against the spending patterns for the income band defining the poverty line in each country in 2011. This information is only available for a few countries and never for 2011. The most widely available information is average consumption as summarized by the UN FAO Food Balances Sheets. I use the balances for 1961, the earliest year available, when many people in developing countries were undoubtedly poor. The first paper to measure poverty globally was Ahluwalia, Carter, and Chenery (1979, p. 4), which set the poverty line at consumption of the 45th percentile in India in the 1970s. This was not far off average consumption in 1961.

Table 8 compares the predictions of the basic model with the 1961 consumption pattern for nineteen countries (data are not available for Lithuania). The correspondence between prediction and behaviour is much higher for the developing countries than for the richer countries. Consider first the total weight of the diet. In the rich OECD countries, actual was 2.89 times predicted; in the middle income OECD countries, the corresponding ratio equalled 1.90, while among the eleven developing countries, actual was only 14% greater than predicted.

LP models also work best for developing countries when the components of the diet are considered. In the developing countries, the model predicts that animal products would amount to 10% of consumption, while average consumption in 1961 was 12%. For fats, the prediction was 2% against a 1961 value of 1%. LP over predicts the consumption of grain and grains–58% against a reality of 41%–with the discrepancy made up with greater

consumption of vegetables and fruits–prediction of 31% versus actual consumption of 40% and 'other product' where the model predicts zero and 1961 consumption was 6%. The latter includes sugar (average of 9 kg per head), which was consumed everywhere, and alcohol (average of 8 kg), which was consumed in significant quantity only in Zimbabwe and Gambia (54 and 40 kg per head respectively).

These predictions are not perfect but are far closer to reality than the predictions for rich countries. For the USA, UK, and France, the prediction is that grain and grain products would amount to 65% of consumption, whereas the actual value in 1961 was 12%. The discrepancies was matched by under predicting the consumption of animal products (15% versus a reality of 40%), fruit and vegetable consumption (16% versus 29%) and the consumption of 'other products (zero versus 18%). The latter consisted mainly of sugar (45 kg per year) and alcoholic drinks (112 kg per year). The big errors for the rich countries illustrate Stigler's point about the failure of linear programming to predict behaviour, while the much smaller errors for developing countries illustrate my point that linear programming can predict fundamental features of the behaviour of the poor.

How well does linear programming perform within the broad categories? Linear programming performs poorly in explaining the variety of foods eaten. This is especially true of fruits and vegetables. Normally, linear programming selects cassava or a single vegetable, which is generally the cheapest source of vitamin C. In reality, people consume many different fruits, nuts, and vegetables. Some of this behaviour is a response to seasonable prices changes, which do not appear in the ICP. A fundamental reason, however, is that many vegetables sell at similar prices and have similar quantities of vitamin C. The diet can be diversified at very little cost. The same is true of some fish and animal products.

On the other hand, the most important food consumed by the poor is grains and grain products, and linear programming correctly predicts the most important grain in eleven of the fourteen developing countries in the sample. Success is high in Africa (millet and sorghum in Niger, maize in Zimbabwe, rice in Liberia, wheat in Algeria and Egypt with some success in predicting grains of secondary importance) and south Asia (Bangladesh, Myanmar, Indonesia, Sri Lanka, and Vietnam all rice).

The model is off the mark in three cases. I tally Thailand as an error since maize is the grain in the linear programming solution, but rice was the predominant crop in 1961. In that year, very little maize was consumed by humans, but now it comprises 10% of grain consumption, presumably eaten by the poor. Linear programming anticipated this development, so perhaps this is not a prediction error at all.

The predictions are most problematic for the biggest countries, China and India, where the model predicts sorghum and millet as the principal grains. In India these crops comprised 22% of grain consumption in 1961 (down to 9% in 2011) and were disproportionately eaten by the poor. The thing is, however, that the poor also consumed large quantities of more expensive wheat and rice, and this behaviour is not captured by the basic model. The situation was similar in China where millet and sorghum comprised 18% of the grain consumed by humans in 1961. Jinqing (2005, pp. 85, 124, 146-7) discusses the widespread consumption of sorghum and other coarse grains by peasants in Henan in 1996, for instance. (Virtually none is eaten today.)

The results for India and China raise several broad questions. The first relates to the ICP data used here. The ICP includes a single price for each item that is supposed to be representative of the whole country. India and China are very large, and their economies not highly integrated. The relative prices in the regions differ from the relative prices shown in the ICP. In that case, it would be better to apply the linear programming approach to sub-

national units, so the baskets would differ in wheat growing districts and rice growing districts, for instance. The same criticism applies to any other approaches (including the World Bank's) that come up with a single basket for large and diverse countries.

The second issue relates to the importance of habit in diet choices. An extreme view would maintain that food choices are entirely driven by customs that have nothing to do with what is cheap. That view is hard to credit for developing countries in view of the results just reported. Atkin (2013, 2016) has proposed a more specific hypothesis that warrants attention. He claims that preferences do reflect local scarcities and these preferences acquire a life of their own, so that they continue to influence behaviour when market integration increases or people migrate to districts where relative prices differ. Migrants continue to purchase the foods to which they are accustomed with the result that their diets cost more than those of their neighbours whose tastes accord with the scarcities of their new homes. Atkin's (2013, p. 1147) analysis of intra-Indian migration suggests that habit raises the cost of calories by about 5% even for deprived groups. A 5% increase in the cost of food would increase the poverty line by about 3% given food's share in expenditure. This is not a large amount in view of the many other uncertainties involved in setting the poverty line. Furthermore, habits decay over time, and people adapt to the new price environment.

Third, there is a question: should we pay attention to food habits in setting the poverty line? The former is a matter of fact, while the latter is a matter of value. Many Indians prefer rice and wheat to millet and sorghum. People in Niger eat nothing but millet and sorghum. Should Indians be given a more costly standard than people in Niger just because they have a taste for more expensive food? The poverty line represents the cost of meeting basic needs, not a level of satisfaction, and should be set accordingly.

On the practical plane, however, it should be noted that the linear programming poverty line is generous enough to allow for a small accommodation of habit or variety in diet. This latitude arises because the requirements for micro nutrients are set at levels that the medical profession judges to be needed for healthy living. These levels exceed intake needed to prevent acute deficiency symptoms, as we have mentioned. People who receive the income to consume the recommended daily allowance of some nutrient might purchase a diet with less than the RDA in order to indulge a taste. This is probably the reason that most of the Indian population is anaemic, for instance. Likewise a calorie standard of 2100 is higher than absolutely necessary for survival, so taste can be indulged at the expense of energy. Poverty is constraining and linear programming captures those bonds, but it is not wholly immobilizing.

Non-food consumption

A poverty budget includes items besides food. In the World Bank approach, non-food expenditure is the average mark-up of non-food spending in the poor countries whose budgets underlie the line. There is no reason to suppose that these mark-ups reflect identical non-food budgets—and, indeed, the claim that "the judgements made in setting the various parameters of a poverty line are likely to reflect prevailing notions of what poverty means in each country setting" (Ravallion, Chen, Sangraula 2009, p. 167)—belies that possibility. Since the poor countries are mainly tropical, the only safe assumption is that the non-food spending is appropriate to tropical conditions.

I address this limitation by setting an explicit non-food budget. It is intentionally

austere and is limited to housing, fuel, lighting, clothing, and soap.¹⁴ The cost of education, medical care, and so forth are not included, so the resulting poverty line is an absolute minimum. Arbitrariness is unavoidable. Our approach makes the decisions visible, so they can be debated, rather than leaving them unexamined under the rubric of "other spending." The linear programming framework could be extended to include the non-foods by specifying the requirements in terms of square metres of living space, BTUs of energy, etc., but the linear programming problem decomposes into separate problems so long as the goods in each category contributed only to meeting the requirement of that category, which is the maintained assumption. So I analyse the categories in turn.

I set the quantity of housing at three square metres per person. By the standards of rich countries, this represents extreme–and often illegal–overcrowding. Even illegally subdivided apartments in New York offer 5-10 sq metres per person (Gadanho 2014, p. 135). Exceptionally high densities, however, are common in Third World slums. In Bombay in 1921, for instance, cotton mill workers lived one family to a room of 13.3 square metres giving each person 2.3 sq metres of space. In Ahmedabad in the 1920s, the average was 3.6 square metres per head, in Shanghai in 1952, the average resident had 3.4 square metres, and in the slums of Nairobi today, the rate is 3 sq metres per person. UN Habitat (2003) proffered a definition of overcrowding as more than 2 people per room or less than 5 sq metres each. In 2010, however, this standard was revised to 3 people per room, implying less than 3.3 square metres per person.¹⁵

To work out the cost of 3 square metres, we need the rent per square metre. For six poor countries (Algeria, Niger, Bangladesh, Indonesia, Sri Lanka, and Vietnam), the ICP reports rents for 'traditional' structures, so rent per square metre can be calculated.¹⁶ For the remaining countries, it was necessary use other sources detailed in the data appendix. The aim was to find market (not subsidized) rents in the poorest districts of the capital or other large cities. In some cases, like New York, rents were found for illegal, substandard apartments, although, in this case, the rent per square did not differ greatly from the US Department of Housing Fair Market Rent for New York County in 2011. Table 10 tabulates the rents. The differences across countries are striking. In most of the poor countries, rents were \$.50 - \$1.00 per square metre per month. Even in China, where the rent is the free market average for the eight largest cities, it came to only \$1.28 per square metre. On the other hand, in the USA, UK, and France, rents were on the order of \$25 per square metre per month. In the USA, rent on 3 square metres worked out to be \$1.76 per day, which shows the impossibility of living on \$1.90.

The requirements of clothing, fuel, and lighting depend on climate. A point of departure for fuel and lighting is the Energy Poverty Line of the Millenium Development

¹⁵Shirras (1923, p. 25), Bombay Labour Office (1928, p. 19), Sun, Linyun (2011, p. 57), UN-Habitat (2003a, p. 237), UN-Habitat (2003b, p.12), UN-Habitat (2010, p. 16).

¹⁶The rents shown in this paper are averages of at least two housing classes. They generally have electricity and indoor water supply. Rents for poorer dwellings lacking electricity and indoor water or for better dwellings, which also have indoor toilets and kitchens, give very similar results in these international comparisons.

¹⁴The soap requirement was arbitrarily set at 1.3 kilograms per year (25 grams per week).

Goals, which sets the minimum at 1.6 million BTUs of fuel and .4 million BTUs for lighting (Modi, McDade, Lallement, and Saghir 2006, p. 9). The former, which is based on engineering studies, provides enough energy for cooking but nothing beyond that for heating, so the requirement is suitable only for hot climates. The latter provides enough energy for three hours of lighting per night from a candle or an electric light bulb. Other sources of information are needed to determine clothing requirements and to extend the fuel and lighting requirements across climate zones. I used household expenditure surveys to set the requirements. In the case of fuel, these are corroborated and extended with engineering calculations.

For the expenditure survey approach, I use Prokopovich's (1909) survey of St Petersburg workers in 1907/8 and Shirras's (1923) survey of workers in Bombay cotton mills in 1921/2. These were chosen to represent opposite ends of the climate spectrum and because the surveys are very early and were taken when the workers were indubitably poor. Both surveys show average spending on clothing, footwear, bedding, fuel, and lighting. The Bombay survey breaks all categories down by income bands, and the St Petersburg survey does the same for clothing, footwear, and bedding. In Bombay the range 30-40 rupees/month was the lowest income band with a large number of workers as was 300-400 rubles/year in St Petersburg. I assume these low income workers were at similar levels of deprivation, so that differences in their expenditures represent responses to climate and not to real income or price differences.¹⁷ For fuel and lighting, the averages for all workers provide a less nuanced basis of comparison.

The surveys reveal much more substantial purchases of clothing, footwear, and bedding in Russia than in India. Both surveys tell us expenditures in money–rupees or rubles. To compare quantities in the two countries, these must be divided by prices. For clothing and related items, the prices of coarse cotton cloth were used as the deflator. In that way we compare expenditures in 'metres of cloth equivalents'. Table 9 shows the results. In St Petersburg, the low wage workers consumed almost three times as many metre-equivalents of clothing, footwear, and bedding as their counterparts in Bombay. Clothing consumption was almost 60% greater, bedding was eight times more–the nights are much colder in Russia than in India–while footwear was, not surprisingly, 27 times greater. Spending on these items increased more with income in Russia than in India. The average family member in St Petersburg consumed almost four times as many metre-equivalents as the average Bombay family member. Much of the extra income went on clothing for which the Russian consumption was three times the India. Living in the northern winter required considerably more clothing.

Similar calculations for lighting and fuel can only be done for the average worker since the Russian survey did not break these expenditures down by income band. Each member of the average working class household in Bombay consumed 0.37 million BTUs of kerosene in lamps (very close to the Millenium Development Goal), while the average household member in St Petersburg consumed 0.87 million BTUs–over twice as much. This looks like the cost of long winter nights.

The disparity was much greater for fuel. In Bombay, fuel consumption averaged 3.15

¹⁷Without the adjustments for climate, the real annual earnings of the average cotton mill operative in Russia in 1907/8 look to have been about 50% higher than that of their counterparts in Bombay in 1921/2. With the climate adjustments, their average real earnings were virtually identical (Allen and Khaustova 2017).

million BTUs per person. Among the low income workers, fuel consumption was only 2.52 million BTUs, marginally greater than the Millennium Development Goal. In Russia, however, average consumption in working class families was 24.62 million BTUs per year–close to 10 times more than in Bombay. One limitation of this calculation is that there was no breakdown of fuel spending by income class in Russia. Judging by clothing, footwear, and bedding, where average spending was double that of the low wage workers, the low wage workers in St Petersburg might have been consuming on the order of 12 million BTUs per person.

We can test this conjecture by approaching the problem from a different perspective. Heating engineers have developed a methodology to calculate the energy required to keep a building at a desired temperature.¹⁸ Critical parameters are the dimensions of the space to be heated, the temperature to be maintained, the pattern of the exterior temperature over the year, and the insulating efficiency of the construction. No matter how many rooms there were in a dwelling, it was normal to heat only one, and we proceed accordingly. On the assumption of 3 square metres per person, a family of four lived in a room of 12 square metres. The room is assumed to have been 3 x 4 metres with a ceiling height of 2.4 metres. The R value of the floor, walls, and ceiling depends on the construction materials used, their thickness, and layering. An R value of 2 is assumed.¹⁹ We assume the room is heated to an internal temperature of 15 degrees centigrade. The external temperature is measured by the 'heating-degree days,' that is, the sum over the year of the difference between the desired internal temperature and the external temperature. We obtained this from the heating industry website <u>http://www.degreedays.net/</u>. This website gives heating degree-days calculated at half hour intervals over five years for most airports and weather stations in the world. The values chosen for the parameters could be debated, but alternatives give similar results. Under the assumptions made, the fuel required per person per year works out to have been 12 million BTUs in St Petersburg and zero in Bombay. For the latter, the appropriate fuel allowance is the 1.6 million BTUs required for cooking in the Energy Poverty Line of the Millennium Development Goals.

Heating degree days were ascertained for major cities in the twenty countries studied here, and heating requirements were then calculated. Requirements were set at these calculated values so long as they exceeded the Millenium Development energy poverty line; otherwise, the poverty line value of 1.6 million BTUs was adopted. Requirements for lighting, clothing, footwear, and bedding were scaled between those for Bombay and St Petersburg in proportion to the heating degree days of the city relative to the difference between Bombay and St Petersburg.

The cost of the requirements for fuel, lighting, clothing, footwear, and bedding can be calculated from the prices of cloth and fuels in the ICP. The cheapest source for each

¹⁸<u>http://hyperphysics.phy-astr.gsu.edu/hbase/thermo/heatloss.html</u> summarizes the basic theory and equations. I am indebted to Michail Moatsos, who has used this methodology in his own work, for bring it to my attention. See Moatsos (2015).

¹⁹For R values of common building materials, see, for instance, <u>http://www.coloradoenergy.org/procorner/stuff/r-values.htm</u> Inspectapedia (2008) assessed an old log cabin with an uninsulated roof, upper exterior walls made of 3/4 inch lumber, and drafty windows as having an R-value of 2 overall. <u>http://inspectapedia.com/structure/Log Home Insulation.php</u>

requirement in each country was used in these calculations.

Basic needs poverty line and the extent of world poverty

The basic needs poverty line (BNPL) is the sum of the cost of the linear programming diet, the non-food costs, and rent. How do the BNPLs compare to the World Bank poverty line? Does the BNPL change our view of global poverty?

To allow comparison with the WBPL of \$1.90 per day, Table 11 shows the values of the BNPLs when they are converted to US dollars in the usual manner. The cost of the BNPL line is greater, the higher is the quality of the diet. The BNPL lines for the OECD countries exceed those of the non-OECD countries for any diet in view of the much higher cost of housing in developed countries²⁰ and the relative coldness of the climate. The CPF line at \$1.84 comes closest to the WBPL for developing countries. The CPF model could be regarded as micro-foundations for the World Bank's line. However, since people eating a CPF diet suffer many nutritional deficiencies, it is not a good poverty line. Instead, the line implied by the basic diet is preferable. Henceforth, I will confine discussion of the BNPL to the version using the basic diet.

Table 12 shows a breakdown of poverty line spending by broad category. In the developing countries, about two-thirds of spending is on food, one quarter on non-foods, and 5-10% on rent. This rent share is consistent with the experience of pre-industrial Europe (Allen 2001). These shares shift dramatically with income. The food share drops to one quarter in the USA, UK, and France, the non-food share remains at one quarter, and the rent share explodes to half or more of income. The very poor in the United States pay this much or more in rent (Desmond 2016).

In Table 13, the expenditures on broad categories of the basic poverty line are converted to US dollars using both the market exchange rate and the PPP exchange rate for individual consumption expenditure by households normally used by the World Bank. The conversion at the market exchange rate shows that food is most expensive in rich countries. The cost of non-food goods is also much greater among the rich than elsewhere due to the colder climate in the USA and northern Europe, and high rents in rich countries mean that spending on housing is an order of magnitude greater than in the developing world. When currencies are converted at PPP, costs rise in the poor countries relative to the rich, and food costs in dollars end up being greater in the poor countries than in the rich. The burden of cold weather and the high cost of housing in rich countries remain, although diminished in relative magnitude.

²⁰The costs per square metre of housing for six of the developing come from ICP2011, as noted, and appear to be 'nationally representative.' The costs for the remaining countries are the costs of poor quality housing in low income districts in large cities. Sensitivity analysis of the impact of this selection procedure was done to see if it affected the BNPL. Halving the cost of such housing in the developing countries, for instance, had only a negligible impact on the BNPL since even expensive urban housing in those countries is very cheap. Since the prices of everything else are 'nationally representative,' the BNPLs for the developing countries also are 'nationally representative.' This, however, is not true in the rich countries where the cost of housing there had a large impact on the BNPL. For the rich countries, the BNPLs must be interpreted as applying to large cities.

The basic needs poverty line cost on average about 40% more than the WBPL in developing countries (Table 11). The dispersion about this average, moreover, is substantial. The basic diet BNPL in several African countries cost less than \$1.90 per day. On the other hand, the basic diet BNPL cost almost twice as much in some south Asian countries and in the rich OECD countries.

The import of these discrepancies is that world poverty is greater than implied by the World Bank Poverty Line and its geographical distribution is different. Table 14 shows head count poverty rates for these countries as implied by the \$1.90 line and by the basic diet BNPL. The headcounts are computed with the World Bank's PovcalNet online calculator and, in the cases of the USA, UK, and France, directly from the national household surveys made available by the Luxembourg Income Study.²¹ The BNPL indicates that there were 50% more poor people than estimated by the World Bank in the 17 countries in the table for which we have estimates. The picture of sub-Saharan Africa does not change much. On the other hand, there are many more poor people in Asia. In India, the increase is 20%, in China 74%, and in Indonesia, Vietnam, and Sri Lanka, the number of poor increases by about three fold. The numbers involved are large, and the head count ratio in Indonesia, for instance, rises from 14% to 46%. Economic growth in Asia has been significant but perhaps not as impressive as it seemed. While the previously noted decline in the consumption of sorghum and millet in India and China suggests the number of poor people is falling, it is still substantial.

Table 14 also reports numbers in absolute poverty in OECD countries. This is a new focus of research and one of considerable importance in view of current interest in inequality in these countries. Edin and Schaefer (2015) estimated that 2.8 million children lived on less than \$2 per day in the USA. Table 11 shows that people cannot survive on \$2 a day since it does not cover the minimum food, clothing, and shelter required in big cities in a cold, rich country. Using the basic needs value of \$3.72 per day for the USA implies that 1.5% of the American population–4.6 million people–lives in absolute poverty. This is marginally more than in the UK (1.25%) and significantly more than France (.63%). If France is representative of western Europe, then extreme poverty looks to be a peculiarly Anglo-American problem.

The role of rent in the BNPLs of rich countries is particularly prominent since their rents are so high. Rents in rural locations in the USA, however, can be very low. In that context, the WBPL offers an insight, for it sets rent close to zero. Even with that reduction, however, there were still 3.6 million people in extreme poverty in the USA in 2011. Country living does not eliminate absolute poverty.

Poverty Purchasing Power Parity

One of the contentious issues that has arisen with the World Bank Poverty line is the exchange rate to use in converting the dollar value of the line into local currencies. The standard World Bank procedure is to use the purchasing power parity (PPP) exchange rate for

²¹<u>www.lisdatacenter.org</u> The samples for 2010 were used, and the 2011 poverty lines were converted to 2010 values with the rates of consumer price inflation in each country. This source was used for USA, UK, and France since the World Bank counsels against using PovcalNet for these countries. PovcalNet gives similar estimates of the number of poor to those computed with lisdatacenter.org, but the latter permits finer measurement.

individual consumption expenditure by households. The spending pattern of the poor differs from the average pattern and so does the spending pattern of developing countries vis-à-vis OECD countries. The question is whether a poverty purchasing power parity (PPPP) exchange rate would give a different conversion.

This issue can be explored with the BNPL's calculated in this paper. In the dual formulation of the standard model of consumer choice, the solution to the problem of minimizing the cost of reaching a specified utility level is the expenditure function, which expresses that cost as a function of the prices of the consumer goods and the specified utility level. If the expenditure function is evaluated at two sets of prices, the ratio of the expenditures in the two cases is the 'true cost of living index': It indicates the relative change in spending needed to compensate the consumer for the differences in prices by keeping him or her at the same level of utility. The solution to the linear programming problem does not give an explicit expenditure function, but it does indicate the cost of meeting the specified requirements at the given prices. The ratio of the costs of meeting the specified requirements at two sets of prices is the linear programming analogue to the true cost of living index. Consequently, when the nutritional requirements are set at poverty levels, that ratio is the true poverty purchasing power parity (PPPP) exchange rate.

It should be noted that the ratio of the costs in the 'true linear programming cost of living index' is not an index number of the orthodox sort. The numerator and the denominator need not have any foods in common, for instance. Uniform requirements ensure comparability as the consumption pattern shifts in response to price differences.

Table 15 shows how the linear programming PPPPs for the various levels of nutritional requirements compare to the household expenditure PPPs. Among the rich OECD countries, the linear programming purchasing power parity exchange rates average close to the exchange rate for household consumption normally used to converted poverty lines between countries. Among the middle income OECD countries and the developing countries, however, the situation is very different. Their PPPP exchange rates are about half to three quarters of the PPP exchange rates for household consumption. Using the household consumption PPP to convert poverty lines gives seriously misleading results.

Conclusion

In this paper we have proposed that poverty lines can be defined by specifying a basic needs basket. Linear programming is used to specify the food component of basic needs. While the diet problem was the first problem ever formulated as a linear programming problem and remains a classic for teaching purposes, the common view amongst economists is that it does not describe anyone's behaviour. While that belief is certainly appropriate for rich people, we have argued that it is not correct for the 'absolute poor'. When people are on the margin of survival, their needs take precedence over their desires, and their behaviour is governed by linear programming. This statement is not unambiguous, however, for a range of nutritional requirements can be imposed on the diet problem. We have argued that the 'basic' requirements-those which supplied adequate amounts of calories, protein, fat, and the vitamins and minerals needed to prevent anaemia, beri-beri, pellagra, and scurvy-imply diets that describe the main features of the diets of the poor. Those diets are based around common grains, legumes, a little milk or fish, oil, and vegetables. Linear programming cannot, however, describe all of the details of the diets.

We have also explicitly budgeted the non-food component of 'basic needs' and expressed many of them as functions of climate. This is important if the poverty line is to be applicable everywhere on the globe since the existing World Bank procedure gives a line which is only appropriate for hot climates. Accomodation rents vary enormously between rich and poor countries, and the basic needs line includes that differential, while the World Bank line does not.

Although the poverty line proposed here is intended to be austere, it does nonetheless provide some latitude for habit and taste since the nutritional requirements are those recommended by the medical profession for 'good health.' This leaves scope for people to trade off some health for customary consumption, sugar, or alcohol, as they prefer. Basic needs are not the same as local taste. However, the trade-offs are limited. That is the nature of poverty.

We argued in the introduction that an international poverty line should satisfy five conditions. The basic needs poverty line meets all of them. First, the line should have a clear meaning related to survival. The BNPL meets this condition since it is defined in terms of the food, fuel, clothing, and shelter requirements to ensure social reproduction and defence against the main deficiency diseases and survival in cold as well as hot countries. Second, the line should represent a constant standard across time and space. This requirement is met by imposing the same or equivalent requirements in all cases. Third, the poverty line should respond to local prices and climate. Indeed, local prices determine the solution to the linear programming along with the nutritional requirements, and non-food consumption varies with climate. Fourth, the poverty line should avoid intractable index number problems. There are no index number problems with the linear programming approach since the solutions to the diet problem are in local prices and the non-food requirements are also costed with local prices. Comparability across countries and over time is guaranteed by using the same requirements everywhere-not by PPP. Fifth, the poverty line should require only readily available information. An ICP data set including relevant accommodation costs would be do the job, although it is not detailed enough for regional breakdowns in large countries.

The basic needs poverty line provides a direct connection between the value of the line and its meaning in terms of human health and social reproduction. Using the BNPL provides a more transparent approach to poverty measurement than existing World Bank procedures. The BNPL indicates that there is considerably more poverty in the countries analysed here–and they include much of the population of the developing world–than the World Bank has counted. The BNPL also indicates there are millions in 'absolute poverty' in rich countries–especially the USA and UK.

1700 Calorie model diets (kilograms per person per year)

			kilograms	per perso	n per yea	r	
	wheat					beans/	
	flour	bread	rice	maize	millet	lentils	oil
developing	countries						
Niger							70
Zimbabwe				178			
Gambia				176			
Liberia			172				
Egypt				172			
Algeria	170						
India							70
China							70
Thailand							70
Indonesia							70
Banglades	sh		172				
Myanmar							70
Sri Lanka			175				
Vietnam							70
middle inc	ome OECD						
Turkey				172			
Mexico				171			
rich OECD) and Euros	tat					
Lithuania	170						
UK	170						
USA							70
France	170						

Total weight of linear programming diets (kilograms per person per year)

	1700	CPF	basic	full course
developing	countries			
Niger	70	187	264	356
Zimbabwe	178	214	325	329
Gambia	176	213	250	325
Liberia	172	197	303	636
Egypt	170	232	265	371
Algeria	172	195	415	471
India	70	191	295	397
China	70	191	250	763
Thailand	70	206	264	275
Indonesia	70	198	330	472
Banglades	172	197	353	406
Myanmar	70	200	249	406
Sri Lanka	175	206	274	433
Vietnam	70	196	271	530
middle inco	ome OECD			
Turkey	172	214	320	386
Mexico	171	195	303	317
_				
rich OECD	and Eurost	tat		
Lithuania	170	195	506	575
UK	170	195	286	371
USA	70	191	278	319
France	170	195	370	388
average	131	200	344	426

Number of items in linear programming diets

	1700	CPF	basic	full course
developing	countries			
Niger	1	2	4	6
Zimbabwe	1	2	5	6
Gambia	1	2	6	6
Liberia	1	3	5	7
Egypt	1	3	5	6
Algeria	1	2	5	6
India	1	2	5	5
China	1	2	4	6
Thailand	1	3	6	7
Indonesia	1	3	6	6
Banglades	1	3	6	6
Myanmar	1	3	6	7
Sri Lanka	1	3	5	5
Vietnam	1	3	6	8
middle inco	ome OECD			
Turkey	1	2	4	6
Mexico	1	2	4	5
rich OECD	and Eurost	tat		
Lithuania	1	2	5	8
UK	1	2	4	7
USA	1	2	4	8
France	1	2	5	7
average	1	2.4	5	6.4

CPF diets

(Kilograms per person per year)

													spinach
wheat				millet &	beans &				cheese &				cauliflower
flour	bread	rice	maize	sorghum	lentils	milk	fish	eggs	beef	oil	potatoes	cassava	peanuts
countries													
				167						20			
			210							4			
			210							3			
		153			33					11			
185										11			
	124		101							7			
177										14			
177										14			
			174		26					5			
		153			34					11			
		153			33					11			
		153			36					11			
		172			26					7			
163		22								11			
me OECD													
147			59							7			
177										18			
and Eurosta	<u>It</u>												
185										11			
185										11			
177										14			
185										11			
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-					1	
	iron	B12	folate	B1 (thiami	niacin	С
developing c	ountries					
Niger	72%	0%	76%	121%	53%	0%
Zimbabwe	93%	0%	76%	180%	82%	0%
Gambia	105%	0%	83%	168%	86%	0%
Liberia	48%	0%	261%	96%	61%	10%
Egypt	80%	0%	349%	240%	142%	0%
Algeria	31%	0%	73%	54%	43%	0%
India	30%	0%	70%	52%	41%	0%
China	30%	0%	70%	52%	41%	0%
Thailand	84%	0%	312%	143%	72%	8%
Indonesia	50%	0%	346%	78%	60%	11%
Bangladesh	48%	0%	261%	96%	61%	10%
Myanmar	71%	0%	223%	64%	49%	0%
Sri Lanka	59%	0%	318%	233%	182%	8%
Vietnam	30%	0%	66%	51%	44%	0%
middle incor	ne OECD					
Turkey	98%	0%	85%	142%	167%	0%
Mexico	239%	0%	1030%	698%	353%	3%
rich OECD a	and Eurosta	<u>it</u>				
Lithuania	31%	0%	73%	54%	43%	0%
UK	117%	0%	781%	337%	193%	0%
USA	117%	0%	781%	337%	193%	0%
France	31%	0%	73%	54%	43%	0%

CPF diet: vitamins and minerals relative to RDA

Table 6 Basic diets (Kilograms per person per year)

														spinach
	wheat				millet &	beans &				cheese &				cauliflower
	flour	bread	rice	maize	sorghum	lentils	milk	fish	eggs	beef	oil	potatoes	cassava	peanuts
developing of	countries													
Niger					186					26	3		50	
Zimbabwe				148	65		70				2			41
Gambia				137	51			7			4		48	2
Liberia			167			82		7			10		38	
Algeria		248				59	70				5			34
Egypt	79			106					35		4			41
India	36				138		70				10			41
China					191					14	4			41
Thailand	17			168		10				14	4			52
Indonesia			145			30		7			6			141
Bangaldesh		33	156			2		7			9			146
Myanmar			92			57		7			1		73	19
Sri Lanka			140			49			35		4			45
Vietnam			82			55		20			3		96	16
middle inco	me OECD													
Turkev	69			124			70				4			53
Mexico				189			70				3			41
rich OECD	and Eurosta	ıt												
Lithuania	75					26		7			11	387		
UK	177						70				8			31
USA	150						67				21			41
France	282					54	0				8			26

27

Table 7 Full course diets (Kilograms per person per year)

														spinach
	wheat				millet &	beans &				cheese &				cauliflower
	flour	bread	rice	maize	sorghum	lentils	milk	fish	eggs	beef	oil	potatoes	cassava	peanuts
developing of	countries													
Niger				149	104		0			26	0		47	30
Zimbabwe				100	103		70				2			53
Gambia					260			5		8	0		12	41
Liberia			37			40		2	24		8		502	24
Algeria		220				49	118				4	43		37
Egypt		126		83		3			35		4			120
India	148				31		70				6			142
China	19				139			41			2			561
Thailand	46			92		20	52			4	3			57
Indonesia			175			11		7			10		53	217
Bangaldesh	1	9	194			12		7			9			175
Myanmar			117			27		7			6		68	181
Sri Lanka			178		3				35		3			214
Vietnam				0		49	16	2	26		2		403	32
middle inco	me OECD													
Turkey	174			20			70				6			117
Mexico				187			70				3			57
rich OECD	and Eurosta	t												
Lithuania	18	_		59		18	43		40		4	376		15
UK	95					65	70				8	94		39
USA	66	33		54		39	67				7			53
France	101	29				72	141				5			40

Table 8 LP predictions compared to 1961 average consumption (Kilograms per person per year)

	total <u>weight</u>	grain/ <u>bread</u>	fats/ <u>oils</u>	animal <u>& fish</u>	veg, nuts <u>& fruit</u>	<u>other</u>
eleven devel	oping cou	ntries				
predicted	293	170	5	28	90	0
1961 average	334	138	4	41	132	19
low income O	ECD					
predicted	312	192	3	7() 47	0
1961 average	593	183	9	147	7 222	32
<u>rich OECD</u>						
predicted	314	203	12	48	3 51	0
1961 average	906	109	17	358	3 259	164

Non-food consumption per head among Workers in Bombay and St Petersburg

	Bombay		St Pete	rsburg
	Low wage	Average	Low wage	Average
clothing, metres)	footwear, bedding	(in cotton	cloth equi	valents,
clothing footwear bedding total	17.00 .59 1.28 18.88	23.13 1.19 3.38 27.69	26.86 16.19 10.08 53.13	62.50 30.63 21.37 114.50
fuel (mBTU) 2.52	3.15		24,62
light (mBT	U) .27	.37		.87
Source: Pr	okopovich (1909)ar	nd Shirras	(1923).	

Housing rents

	\$/sq met/	\$/person/
developing countries	month	year
Niger	0.53	19.07
Zimbabwe	0.69	24.84
Gambia	0.50	18.00
Liberia	1.00	36.00
Egypt	0.84	30.18
Algeria	1.06	38.21
India	0.54	19.27
China	1.28	46.24
Thailand	3.13	112.67
Indonesia	1.99	71.64
Bangladesh	0.31	11.31
Myanmar	0.50	18.00
Sri Lanka	0.31	11.08
Vietnam	1.79	64.32
middle income OECD		
Turkey	2.28	81.91
Mexico	5.00	180.00
rich OECD and Eurost	tat	
Lithuania	1.18	42.32
UK	21.36	768.84
USA	17.94	645.83
France	25.51	918.43
L		07.00
developing	1.03	37.20
middle income OECD	3.64	130.96
rich OECD Eurostat	16.50	593.86

		1700 cal	CPF	basic	full course
	developing co	ountries			
	Niger	0.91	1.15	1.86	2.39
	Zimbabwe	0.88	0.98	1.74	1.86
	Gambia	1.10	1.25	1.46	2.20
	Liberia	1.74	2.18	3.20	6.08
	Egypt	2.12	2.42	3.19	3.45
	Algeria	1.67	1.85	3.05	3.44
	India	1.33	1.52	2.03	2.42
	China	1.60	1.83	2.39	3.38
	Thailand	2.20	2.83	3.48	3.78
	Indonesia	1.85	2.43	3.25	3.35
	Bangladesh	1.12	1.36	1.87	1.88
	Myanmar	2.22	2.74	3.31	3.77
	Sri Lanka	1.11	1.44	2.43	2.96
	Vietnam	1.75	2.30	3.55	4.10
	middle incom	e OECD			
	Turkey	1.49	1.64	2.09	2.28
	Mexico	1.51	1.74	2.00	2.03
	rich OECD ar	nd Eurostat			
	Lithuania	3.63	3.77	4.62	5.17
	UK	3.14	3.21	3.49	4.24
	USA	3.27	3.42	3.72	4.28
	France	3.31	3.38	4.02	4.46
developir	ng	1.54	1.88	2.63	3.22
middle ir	ncome OECD	1.50	1.69	2.05	2.15
rich OE0	CD Eurostat	3.34	3.45	3.96	4.54
		1.24	1.35	1.72	2.09

Linear Program Poverty Lines converted to US dollars per day at PPP

Table 12 Expenditure Breakdown of Basic Needs Poverty Line

developing countries	Food %	Nonfood%	Housing%
Niger	66%	28%	6%
Zimbabwe	69%	24%	7%
Gambia	61%	30%	9%
Liberia	68%	26%	5%
Egypt	68%	24%	9%
Algeria	69%	23%	8%
India	62%	30%	8%
China	52%	39%	9%
Thailand	57%	21%	21%
Indonesia	62%	25%	13%
Bangladesh	64%	31%	5%
Myanmar	53%	42%	4%
Sri Lanka	81%	16%	3%
Vietnam	66%	21%	13%
middle income OECD			
Turkey	54%	30%	16%
Mexico	47%	18%	34%
rich OECD and Eurost	tat		
Lithuania	33%	63%	3%
UK	16%	34%	50%
USA	26%	27%	48%
France	23%	26%	51%
developing	0.64	0.27	0.09
middle income OECD	0.51	0.24	0.25
rich OECD Eurostat	0.25	0.37	0.38

Expenditures by Category in US Dollars at market and PPP exchange rates

	-						
		market	market	market	PPP	PPP	PPP
		\$/year	\$/year	\$/year	\$/year	\$/year	\$/year
developing of	countries	Food	Nonfood	Housing	Food	Nonfood	Housing
Niger		216	93	19	446	192	39
Zimbabwe		235	82	25	438	152	46
Gambia		119	59	18	323	159	49
Liberia		454	174	36	799	306	63
Egypt		239	83	30	789	276	100
Algeria		334	113	38	766	259	88
India		148	71	19	462	220	60
China		260	194	46	454	339	81
Thailand		307	115	113	730	272	267
Indonesia		343	139	72	736	298	154
Bangladesh		147	70	11	439	208	34
Myanmar		217	172	18	643	511	53
Sri Lanka		273	55	11	715	143	29
Vietnam		316	101	64	850	271	173
middle inco	me OECD						
Turkey		285	161	82	412	232	118
Mexico		249	97	180	346	135	250
rich OECD :	and Eurost	at			 		
Lithuania		406	764	42	 565	1062	59
UK		254	520	769	 210	429	635
USA		347	366	646	347	366	646
France		415	458	921	 339	374	753
developing		258	109	37	614	258	88
middle inco	me OECD	267	129	131	379	183	184
rich OECD	Eurostat	356	527	594	365	558	523
() () () () () () () () () ()							

Head	Count	Poverty	Rates
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	percent below povery line		e million	s of poor	population	
	BNPL	WBPL	BNPL	WBPL	millions	
developing countries						
Niger	48.84%	50.34%	8	.28 8.53	17	
Zimbabwe	17.95%	21.40%	2	.56 3.05	14	
Gambia	32.88%	45.29%	0	.44 0.61	1	
Liberia	90.37%	68.64%	3	.18 2.42	4	
India	25.56%	21.23%	322	.97 268.26	1264	
China	13.71%	7.90%	184	.28 106.19	1344	
Thailand	1.94%	0.04%	1	.30 0.03	67	
Indonesia	46.25%	13.58%	113	.22 33.25	245	
Bangladesh	17.65%	18.52%	26	.76 28.08	152	
Sri Lanka	6.24%	2.41%	1	.26 0.48	20	
Vietnam	16.35%	4.78%	14	.21 4.16	87	
middle income OECD						
Turkey	0.73%	0.28%	0	.54 0.21	74	
Mexico	6.28%	3.80%	7	.45 4.51	119	
rich OECD and Eurostat	t					
Lithuania	3.80%	0.87%	0	.12 0.03	3	
UK	1.25%	0.93%	0	.79 0.59	63	
USA	1.50%	1.17%	4	.64 3.61	309	
France	0.63%	0.43%	0	.41 0.28	65	
developing.	0.00	0.02	670	47 455.05	2014	
middle income OECD	0.29	0.23	6/8	47 455.05	3214	
rich OECD Eurostat	0.04	0.02	5	96 4.71	192	
overall	0.06	0.06	692	.41 464.27	3847	

Note: PovcalNet does not generate poverty estimates for Algeria, Egypt, or Myanmar. The figures for the UK, USA, and France were computed from the 2010 household surveys in the Luxembourg Income Survey Cross-National Data Centre http://www.lisdatacenter.org/

1700 cal CPF basic full course developing countries 0.28 0.34 0.50 0.56 Niger Zimbabwe 0.27 0.29 0.47 0.43 0.34 0.36 0.39 0.51 Gambia 0.53 0.86 1.42 Liberia 0.64 0.65 0.71 0.86 0.81 Egypt 0.51 0.54 0.82 0.80 Algeria 0.41 0.44 0.55 0.56 India China 0.49 0.53 0.64 0.79 Thailand 0.67 0.83 0.93 0.88 0.57 0.78 Indonesia 0.71 0.87 Bangladesh 0.34 0.40 0.50 0.44 Myanmar 0.68 0.80 0.89 0.88 Sri Lanka 0.34 0.69 0.42 0.65 Vietnam 0.53 0.67 0.95 0.96 middle income OECD Turkey 0.46 0.48 0.56 0.53 Mexico 0.46 0.51 0.54 0.47 rich OECD and Eurostat 1.24 1.21 Lithuania 1.11 1.10 UK 0.96 0.94 0.94 0.99 USA 1.00 1.00 1.00 1.00 France 1.01 0.99 1.08 1.04 0.75 developing 0.47 0.55 0.71 middle income OECD 0.46 0.49 0.55 0.50 rich OECD Eurostat 1.02 1.01 1.06 1.06

Linear Programming PPPP relative to Individual Consumption PPP

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Appendix

Notes on the linear programming

The following foods were represented in the objective function (equation 1) in the linear programs:

wheat flour, wheat bread, rice, maize flour, oatmeal, beans, eggs, cheese, chicken, milk, meat, fish, butter, margarine, vegetable oil, white sugar, potatoes, tomatoes, cucumbers, cabbage, sweet potatoes, carrots, onions, cauliflower, spinach, ginger, roasted peanuts, avocado, mushrooms, cassava, tofu, alcohol

In addition, the programs for Africa also included millet, millet flour, red sorghum grains, yellow maize grains, and white maize grains

When prices for items in this list were not available in a country, they were excluded from the choice options in the linear program.

Generally, the nutritional composition of foods are coded per 'edible portion.' In the requirement inequalities in the linear programs (equation 2), the nutritional compositions reported in the databases like the USDA *National Nutrient Database* were multiplied by the percentage of the food that is edible (ie allowing for bones, etc), so that the solution of the linear program was the weight of food purchased at the prices specified in ICP2011.

The ICP contains many foods, most of which are clearly too expensive to be chosen by the linear program. For instance, thirteen different kinds of fresh fish or seafood are listed in the core price list of ICP2011, although not all prices are available in all countries. The fish that was cheapest in terms of its nutritional content (allowing for losses in bones, fins, etc) was used in the linear program. This was usually mackerel or tilapia or carp. Similar selections were made for meat, bread, and alcohol in terms of alcohol content. The African regional price list contains a great variety of local alcoholic beverages, which were also investigated to find the cheapest source of alcohol.

Sometimes ICP2011 reported prices for goods that could not have been widely available. Thus, there is a price for mackerel in Zimbabwe. At that price, mackerel is included in the least cost diet. It is so implausible, however, that mackerel is widely available in Zimbabwe that it was excluded from the choice options for that country. Similar exclusions were made in some other cases when it was deemed that the food in question was not widely available.

Online data sources

While the ICP is a tremendous achievement, it is not complete, so it was necessary to add missing variables derived from extraneous sources. Some important additions included:

- the price of wheat flour. Wheat flour is of great importance in poverty measurement, but it was curiously missing from the data for the United States. This was particularly important since conversion to US dollars is a key part of the World Bank's exercise. Why the price is missing is altogether puzzling since it is available on the US Bureau of Labor Statistics website.²² That price was used in the calculations reported here. Wheat flour prices were also taken from the national online retail price databases for some other countries.
- the price of cabbage. This turns out to be important since it is the cheapest source of vitamin C in many places. It was also missing from the USA data in the ICP2011 and the price was taken from the BLS database. In the case of some countries like the UK, the price of cabbage in 2011, which was missing, was estimated from relative prices in 2015 taken from supermarket databases. The same relatives were assumed to obtain in 2011.
- some missing USA and UK prices (like toilette soap, maize flour, and oatmeal in the USA) were taken from data collected in 2011 from supermarket web sites for earlier investigations.
- the price of electricity. This was necessary for the non-food component of the problem. ICP2011 lacks electricity prices for many south and east Asian countries. These were taken from the online tariffs of their electricity suppliers²³. Information for some countries in 2011 was provided by Mr. Beni Suryadi of the ASEAN Centre for Energy, and his help is grateful acknowledge.
- The price of kerosene was missing for many OECD countries. Prices of kerosene or 'light fuel oil for households' were taken from IEA (2012).
- the rental price per square metre of housing. ICP 2011 inquired about rents, but data are available for only six countries in the sample (Algeria, Niger, Bangladesh, Indonesia, Sir Lanka, and Vietnam.) For these the price per square metre of a 'typical traditional dwelling,' generally supplied with electricity and indoor water, but no private toilet, private kitchen, or air conditioning, was used. For other countries, rents were obtained for low standard accommodation in poor districts in large or capital cities was obtained.

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Housing rents

The rental price per square metre of housing was needed to compute the cost of the subsistence requirement for housing of 3 square metres per person.

For Algeria, Niger, Bangladesh, Indonesia, Sir Lanka, and Vietnam, rents were calculated from ICP2011 core price list. The core list indicates rental prices for a variety of units. I used the price per square metre of a 'typical traditional dwelling,' generally supplied with electricity and indoor water, but no private toilet, private kitchen, or air conditioning. These are apparently 'nationally representative.'

Rents for other countries were derived from other sources. The aim was to find rents for low quality accommodation in poor districts in large or capital cities. It was not always possible to find 2011 rents, in which case, a rental price index was used to work out a 2011 value. The following sources were consulted:

Zimbabwe–*African Housing Finance Yearbook* 2015, p. 213. Rent is for 2014 and was assumed to apply to 2011 due to overall price stability.

Gambia–assumed to be \$.50/sq metre/month, which is typical of such a poor country. Liberia–Oshodi (2011, p. 7) Single room without sanitation facilities rents for \$10 per month at low end of distribution. Assumed to be 10 square metres. Egypt–Sabry (2010).

India-rent per square foot of a shanty in Dharavi slum, Siddiqui (2015)

China–Logan, Fang, and Zhang (2009, p. 921) average cost per square metre at 'market rental' in eight largest cities in China from 2000 census. Adjust to 2011 prices with urban housing rental index component of Chinese consumer price index from www.stats.gov.cn Thailand–Aichholz (2016, p.7) deflated with index on page 5.

Myanmar–assumed to be \$.50/sq metre/month, which is typical of such a poor country. Deflated to 2011 with the housing component of India consumer price index.

Turkey–price per square metre from rent of 120 sq metre apartment in Kadikoy district in Istanbul in 2016 from <u>www.globalpropertyguide.com/Europe/Turkey/Rental-Yields</u> Deflated to 2011 with rental price index for Istanbul in numbeo.com.

Mexico-assumed to be \$5 per square metre per month.

Lithuania–rent per square metre in Paneriai district of Vilnius, the most impoverished, from vddv.library.lt

USA–rent taken to be \$1250 per month for a one bedroom slum apartment of 750 square feet (Godanho 2014). The rent is very close to that give in US Department of Housing, Fair Market Rent database for New York County, NY in fiscal year 2011.

UK–rent for one bedroom flat, lower quartile, in Bexley, the cheapest London district, in 2011 from www.gov.uk/government/statistics/private-rental-market-statistics-england-only Flat assumed to be 45 square metres following Roberts-Hughes (2011, pp. 23).

France–rent per square metre in 2015 from cheapest category apartment in 18th arrondissement in Paris from www.lacoteimmo.com/prix-de-l'immo/location/ile-de-france/paris/paris-18eme/750118.htm Deflated from2011 with price index for one bedroom flat outside of city centre for Paris in numbeo.com